

Separation Science - Chromatography Unit
Thomas Wenzel
Department of Chemistry
Bates College, Lewiston ME 04240
twenzel@bates.edu

LIQUID-LIQUID EXTRACTION

Before examining chromatographic separations, it is useful to consider the separation process in a liquid-liquid extraction. Certain features of this process closely parallel aspects of chromatographic separations. The basic procedure for performing a liquid-liquid extraction is to take two immiscible phases, one of which is usually water and the other of which is usually an organic solvent. The two phases are put into a device called a separatory funnel, and compounds in the system will distribute between the two phases. There are two terms used for describing this distribution, one of which is called the **distribution coefficient (D_C)**, the other of which is called the **partition coefficient (D_M)**.

The distribution coefficient is the ratio of the concentration of solute in the organic phase over the concentration of solute in the aqueous phase (the V-terms are the volume of the phases). This is essentially an equilibration process whereby we start with the solute in the aqueous phase and allow it to distribute into the organic phase.

$$\text{solute}_{\text{aq}} = \text{solute}_{\text{org}}$$

$$D_C = \frac{[\text{solute}]_{\text{org}}}{[\text{solute}]_{\text{aq}}} = \frac{\text{mol}_{\text{org}}/V_{\text{org}}}{\text{mol}_{\text{aq}}/V_{\text{aq}}} = \frac{\text{mol}_{\text{org}} \times V_{\text{aq}}}{\text{mol}_{\text{aq}} \times V_{\text{org}}}$$

The distribution coefficient represents the equilibrium constant for this process. If our goal is to extract a solute from the aqueous phase into the organic phase, there is one potential problem with using the distribution coefficient as a measure of how well you have accomplished this goal. The problem relates to the relative volumes of the phases. For example, suppose the volume of the organic phase was very small compared to the volume of the aqueous phase. (Imagine using 100 mL of organic solvent relative to a volume of water equal to that in an Olympic-sized swimming pool). You could have a very high concentration of the solute in the organic phase, but if we looked at the amount of solute in the organic phase relative to the amount still in the water, it might only be a small portion of the total solute in the system. Since we really want as much of the solute in the organic phase as possible, this system has not yet achieved that outcome.

The partition coefficient is the ratio of the moles of solute in the two phases, and is a more effective means of measuring whether you have achieved the desired goal. The larger the value of D_M , the more of the solute we have extracted or partitioned into the organic phase.

$$D_M = \frac{\text{mol}_{\text{org}}}{\text{mol}_{\text{aq}}}$$

Note as well how we can relate D_C to D_M :

$$D_C = \frac{\text{mol}_{\text{org}} \times V_{\text{aq}}}{\text{mol}_{\text{aq}} \times V_{\text{org}}} = D_M \left(\frac{V_{\text{aq}}}{V_{\text{org}}} \right)$$

From experience you have probably had in your organic chemistry lab, you know that the approach that is often used in liquid-liquid extraction is to add some organic phase, shake the mixture, and remove the organic phase. A fresh portion of the organic phase is then added to remove more of the solute in a second extraction. As we will see shortly, this distribution of a solute between two immiscible phases forms the basis of chromatographic separations as well.

Next we want to examine some general types of extraction procedures that are commonly used. The first is a classic example of an extraction procedure that can be used to separate acids, bases, and neutrals.

An aqueous sample contains a complex mixture of organic compounds, all of which are at trace concentrations. The compounds can be grouped into broad categories of organic acids, organic bases and neutral organics. The desire is to have three solutions at the end, each in methylene chloride, one of which contains only the organic acids, the second contains only the organic bases, and the third contains only the neutrals. Devise an extraction procedure that would allow you to perform this bulk separation of the three categories of organic compounds.

Two things to remember:

- Ionic substances are more soluble in water than in organic solvents.
- Neutral substances are more soluble in organic solvents than in water.

The key to understanding how to do this separation relates to the effect that pH will have on the different categories of compounds.

Neutrals – Whether the pH is acidic or basic, these will remain neutral under all circumstances.

Organic acids – RCOOH

At very acidic pH values (say a pH of around 1) – these are fully protonated and neutral

At basic pH values (say a pH of around 13) – these are fully deprotonated and anionic

Organic bases – R₃N

At very acidic pH values (say a pH of around 1) – these are protonated and cationic

At very basic pH values (say a pH of around 13) – these are not protonated and neutral

Step 1: Lower the pH of the water using concentrated hydrochloric acid.

Neutrals – neutral

Acids – neutral

Bases – cationic

Extract with methylene chloride – the neutrals and acids go into the methylene chloride, the bases stay in the water.

Step 2: Remove the water layer from step (1), adjust the pH back to a value of 13 using a concentrated solution of sodium hydroxide, shake against methylene chloride, and we now have a solution of the organic bases in methylene chloride. (SOLUTION 1 – ORGANIC BASES IN METHYLENE CHLORIDE)

Step 3: Take the methylene chloride layer from step (1) and shake this against an aqueous layer with a pH value of 13 (adjusted to that level using a concentrated solution of sodium hydroxide).

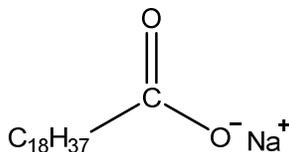
Neutrals – neutral

Organic acids – anionic

The neutrals stay in the methylene chloride layer. (SOLUTION 2: NEUTRALS IN METHYLENE CHLORIDE) The acids go into the water layer.

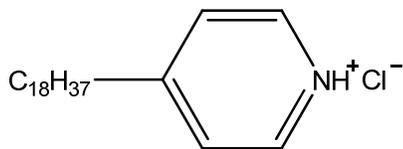
Step 4. Take the water layer from Step (3), lower the pH to a value of 1 using concentrated hydrochloric acid, shake against methylene chloride, and the neutral organic acids are now soluble in the methylene chloride (SOLUTION 3: ORGANIC ACIDS IN METHYLENE CHLORIDE).

Devise a way to solubilize the organic anion shown below in the organic solvent of a two-phase system in which the second phase is water. As a first step to this problem, show what might happen to this compound when added to such a two-phase system.

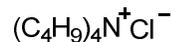


This compound will align itself right along the interface of the two layers. The non-polar C_{18} group is hydrophobic and will be oriented into the organic phase. The polar carboxylate group is hydrophilic and will be right at the interface with the aqueous phase.

One way to solubilize this anion in the organic phase is to add a cation with similar properties. In other words, if we added an organic cation that has a non-polar R group, this would form an ion pair with the organic anion. The ion pair between the two effectively shields the two charged groups and allows the pair to dissolve in an organic solvent. Two possible organic cations that could be used in this system are cetylpyridinium chloride or tetra-n-butylammonium chloride.



cetyl pyridinium chloride



tetra-n-butylammonium chloride

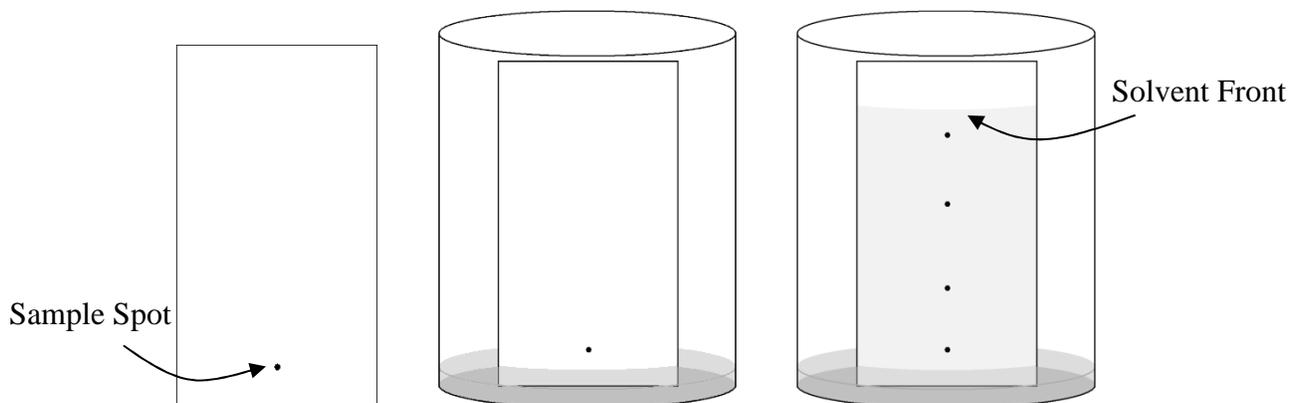
A somewhat similar procedure can often be used to extract metal complexes into an organic phase. Metal salts with inorganic anions (halide, sulfate, phosphate, etc.) are generally water-soluble but not organic-soluble. It is possible to add a relatively hydrophobic ligand to the system. If the ligand complexes with the metal ion, then the metal complex may be organic-soluble. Usually it helps to form a neutral metal complex. Also, remember back to our examination of the effect of pH on the complexation of metal ions with ligands. The extraction efficiency of a metal ion in the presence of a ligand will depend on the pH of the aqueous phase. Adjustment of the pH is often used to alter the selectivity of the extraction, thereby allowing different metal ions to be separated.

CHROMATOGRAPHY

Chromatography refers to a group of methods that are used as a way of separating mixtures of compounds into their individual components. The basic set up of a chromatographic system is to have two phases, one stationary and one mobile. A compound, which we will usually call the solute, is introduced into the system, and essentially has a choice. If it is attracted to the mobile phase (has van der Waal attractions to the mobile phase), it will move through the system with the mobile phase. If it is attracted to the stationary phase, it will lag behind. It's easy to imagine some solute compounds with some degree of attraction for both phases, such that these move through the system with some intermediate rate of travel.

The first report of a chromatographic application was by Mikhail Tswett, a chemist from Estonia, in 1903. (A list of important literature articles is provided at the end). Undoubtedly other people had observed chromatography taking place, but no one until Tswett recognized its applicability for the separation of mixtures in chemistry. Tswett was interested in separating the pigments in plants. He packed a glass column that might have been comparable to a buret with starch, mashed up the plant and extracted the pigments into a solvent, loaded the solution onto the top of the starch column, and ran a mobile phase through the starch. Eventually he saw different color bands separate on the column, hence the term chromatography. Rather than eluting the colored bands off of the column, he stopped it, used a rod to push out the starch filling, divided up the bands of color, and extracted the individual pigments off the starch using an appropriate solvent. Tswett used a solid stationary phase (starch) and a liquid mobile phase.

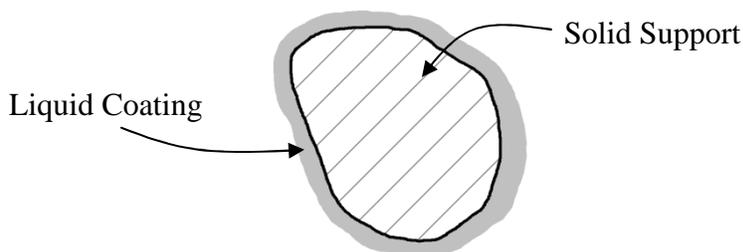
Chromatographic systems can use either a gas or liquid as the mobile phase. Chromatographic systems can use either a solid or liquid as the stationary phase. A solid stationary phase is easy to imagine, as we have already seen for Tswett's work. Another common example is to use paper as the solid (actually, paper is made from a compound called cellulose). The sample is spotted onto the paper as shown below, and the bottom of the piece of paper is dipped into an appropriate liquid (note that the spot is above the liquid). The liquid mobile phase moves up the paper by capillary action, and components of the mixture can separate into different spots depending on their relative attraction to the cellulose or chemicals that make up the liquid.



Another type of chromatography that you may be familiar with is thin layer chromatography (TLC). This is very similar to paper chromatography, although the stationary phase is usually a coating of small particles of a material known as silica gel (silica gel is a polymer with the formula SiO_2 , although a bit later we will talk in more detail about the exact chemical nature of this material) on a glass or plastic plate. Similarly, we could take these silica gel particles and pack them into a glass column, and then flow a liquid through the column. If we used some gas pressure to force the liquid through the silica gel column more quickly, we would have a common technique known as flash chromatography that synthetic chemists use to separate relatively large amounts of materials they have prepared. Another common solid to use in column chromatography is alumina (Al_2O_3 is the general formula, although we will say more later about its exact chemical nature).

These methods we have just been talking about are examples of liquid-solid chromatography. If we used gas as the mobile phase, injected either a gaseous sample or liquid sample into a high temperature zone that flash volatilized it, with some solid as the stationary phase (there are a range of possible materials we could use here), we could perform gas-solid chromatography. If we thought about how a solute compound would interact with such a solid stationary phase, we would realize that it must essentially “stick” to the surface by some intermolecular (van der Waal) forces. This sticking process in chromatography is known as **adsorption**.

Earlier I said that it is also possible to use a liquid as the stationary phase. This might seem odd at first, because it would seem as if the flowing mobile phase would somehow push along a liquid stationary phase. The way to use a liquid as the stationary phase is to coat a very thin layer of it onto a solid support, as illustrated below.



The liquid coating has some attractive forces for the underlying solid surface, such that it sticks to the surface and stays in place. We could probably see how we could easily have a gas flowing around a packed bed of such particles and, so long as the liquid coating did not evaporate, it would stay in place on the particles. Flowing a liquid around it might be a bit more problematic, and we will examine that in length later in this unit. Suffice it to say, though, that it can be done. This would lead to gas-liquid and liquid-liquid chromatographic methods. The interaction of a solute compound with a liquid stationary phase is different than with the solid stationary phases discussed above. It will still depend on having attractive intermolecular forces, but instead of sticking to the solid surface by adsorption, the solute molecule will now dissolve into the liquid stationary phase. If a solute molecule dissolves into a liquid stationary phase in a chromatographic system, we say that the molecule **partitions** between the two phases.

These two terms are so important in chromatographic systems that it is worth summarizing them again:

Adsorption – describes the process of a solute molecule adhering to a solid surface

Partition – describes the process of a solute molecule dissolving into a liquid stationary phase

There are two terms we can describe in chromatography that are analogous to those we already described for liquid-liquid extraction. One of these is the **distribution constant (K_C)** that is the ratio of the concentration of the solute in the stationary phase (C_S) to that in the mobile phase (C_M).

$$K_C = \frac{C_S}{C_M} = \frac{\text{mol}_S/V_S}{\text{mol}_M/V_M} = \frac{\text{mol}_S \times V_M}{\text{mol}_M \times V_S}$$

But just like in liquid-liquid extraction, a problem with this ratio is that the volumes of the stationary and mobile phases might be significantly different from each other. With a solid stationary phase, V_S is comparable to the surface area of the particles. With a liquid stationary phase, the coating is usually so thin that V_M would be much larger than V_S . In many cases, a more useful term is the **partition coefficient (K_X)**, which is the ratio of the moles of solute in each of the two phases.

$$K_X = \frac{\text{mol}_S}{\text{mol}_M}$$

Notice that we can relate K_C to K_X because the mole ratio shows up in both. That allows us to write the following:

$$K_C = K_X \left(\frac{V_M}{V_S} \right)$$

There are also some other fundamental figures of merit that we often use when discussing chromatographic separations. The first is known as the **selectivity factor (α)**. In order to separate two components of a mixture, it is essential that the two have different distribution or partition coefficients (note, it does not matter which one you use since the volume terms will cancel if K_C is used). The separation factor is the ratio of these two coefficients, and is always written so that it is greater than or equal to one. K_2 represents the distribution coefficient for the later eluting of the two components.

$$\alpha = \frac{K_2}{K_1}$$

If $\alpha = 1$, then there will be no separation of the two components. The larger the value of α , the greater the separation. One thing to realize is that there is some limit as to how large we want an α -value to be. For example, the chromatogram in figure (b) below has a much greater α value than that in (a). But the two components are fully separated so that the extra time we would need to wait for the chromatogram in (b) is undesirable. In most chromatographic separations, the goal is to get just enough separation, so that we can keep the analysis time as short as possible.

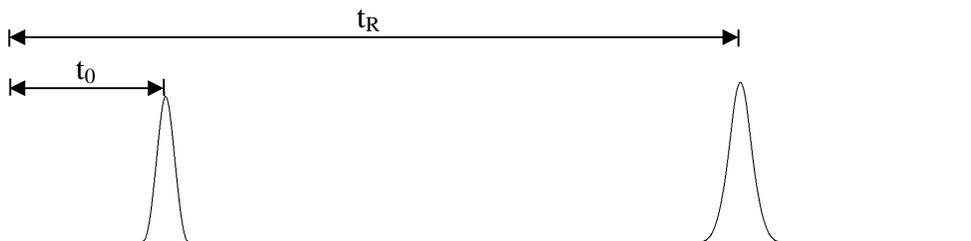


Another important figure of merit in chromatographic separations is known as the **capacity factor (k')**. Capacity is a measure of the retention of a solute, or how much attraction the solute has for the stationary phase. The capacity factor is actually identical to the partition coefficient.

$$k' = \frac{\text{mol}_S}{\text{mol}_M} = \frac{C_S V_S}{C_M V_M} = K_C \left(\frac{V_S}{V_M} \right)$$

We can determine k' values from a chromatogram using the following equation:

$$k' = \frac{t_R - t_0}{t_0}$$

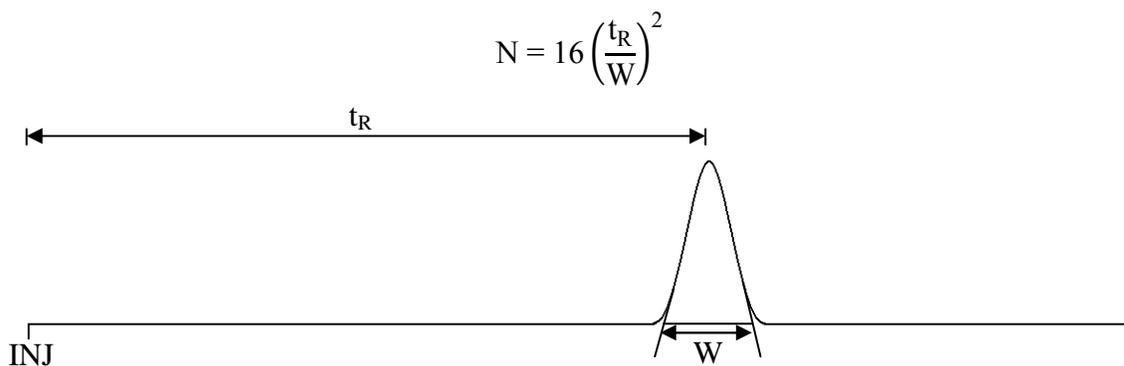


The term t_R is the retention time of the compound of interest, whereas t_0 refers to the retention time of an unretained compound (the time it takes a compound with no ability to partition into or adsorb onto the stationary phase to move through the column). Since t_0 will vary from column to column, the form of this equation represents a normalization of the retention times to t_0 .

Another important figure of merit for a chromatographic column is known as the number of **theoretical plates (N)**. It turns out that one helpful way to think of a chromatographic column is as a series of microscopically thin plates as shown below. Using this picture, we could imagine



a compound moving down the column as a series of steps, one plate at a time. The compound enters a plate, distributes according to its distribution coefficient between the stationary and mobile phase, and then moves on to the next plate. Now it turns out that chromatographic systems never really reach equilibrium, and in fact are not steady state systems, but things like the distribution and partition coefficients, which are equilibrium expressions, are useful ways to examine the distribution in chromatographic systems. A compound with less favorable solubility in the stationary phase would then move through the series of plates faster. The only way to separate two compounds is to have enough plates, or enough equilibrations, to exploit the difference in partition coefficients between the two compounds. A column with more theoretical plates is more likely to separate two compounds than one with fewer. We can determine the number of plates for a compound as shown below.

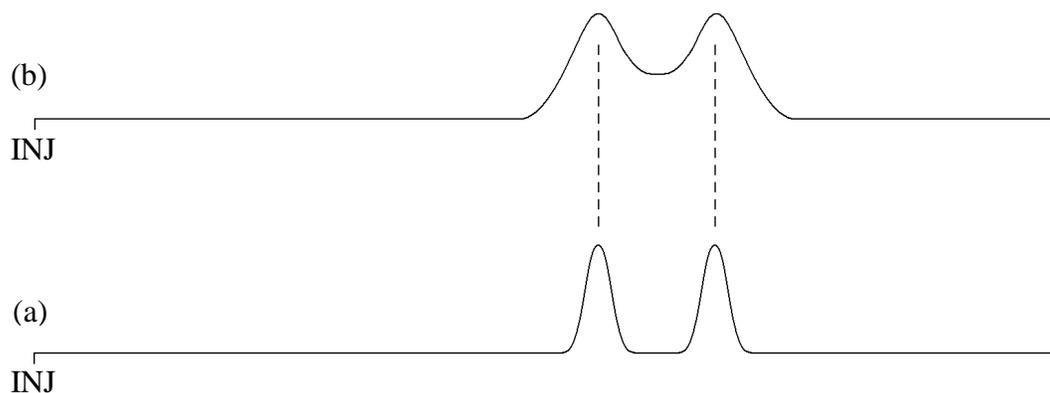


W is the width of the peak where it intersects with the baseline. The important thing to remember is to use the same units when measuring W and t_R (e.g., distance in cm on a plot, time in seconds, elution volume in mL – which is common in liquid chromatography). It should be pointed out that a column will have a set number of plates that will not vary much from

compound to compound. The reason for this is that a compound with a longer retention time will exhibit a larger peak width, such that the ratio term is correcting for these two effects. If we determine the number of plates for a column, dividing the column length (L) by the number of plates leads to the **height equivalent to a theoretical plate (H)**. Note that the smaller the value of H the better. It actually turns out the H is the important figure of merit for a column.

$$H = \frac{L}{N}$$

The chromatograms below show the distinction between a column with a small value of H (a) and one with a much larger value of H (b).



Usually today, though, people refer to something called the **reduced plate height (h)** for a column. The reduced plate height is defined as shown below, in which d_p is the particle diameter of the packing material used in the column (or the internal tube diameter if an open tubular capillary column is used).

$$h = \frac{H}{d_p}$$

You will also come across a term known as the **reduced velocity (v)** in the chromatographic literature. The reduced velocity is defined as follows, in which v is the mobile phase velocity, and D_M the diffusion coefficient of the solute in the mobile phase.

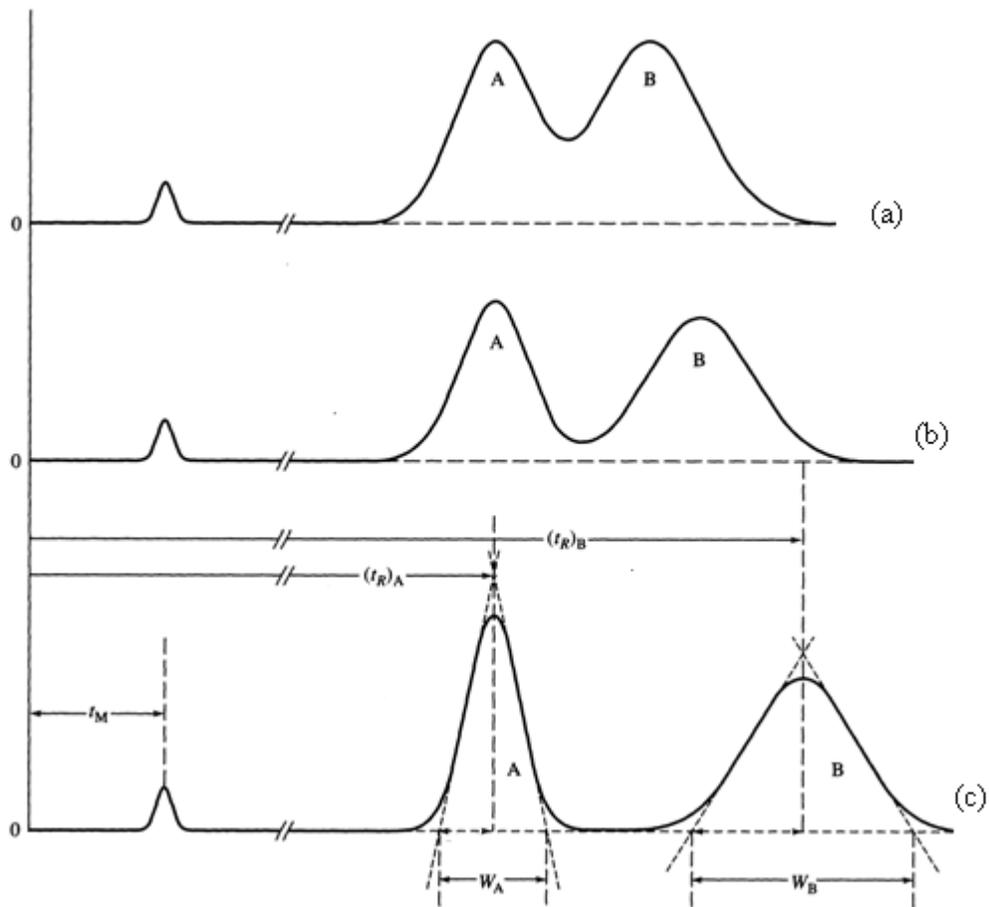
$$v = \frac{d_p \times v}{D_M}$$

Finally, we can define an equation for the **resolution (R_S)** of two compounds. This will be a measure of how much two compounds in a chromatogram are separated from each other.

$$R_S = \frac{2(t_2 - t_1)}{W_1 + W_2}$$

The terms t_2 and t_1 refer to the retention time of the two compounds, and W_1 and W_2 to the width of each peak at baseline.

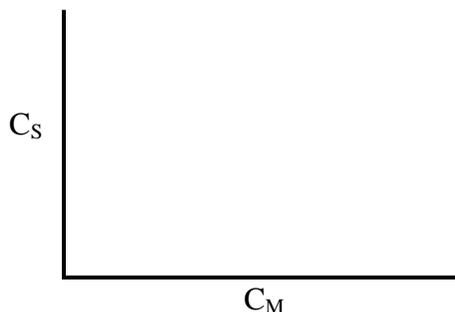
The figure below shows the separation of two peaks at resolution values of 0.75 (Figure a), 1.0 (Figure b) and 1.5 (Figure c). The better separation of A and B that occurs with increasing resolution is obvious. It is also worth noting that the analysis time is longer the higher the resolution. Chromatographic analyses are always a compromise between the degree of separation of the peaks and how long it takes to perform the analysis. In many cases, the goal is to get just enough separation in the shortest period of time.



Distribution Isotherms (Isotherm means constant temperature):

We have used the distribution and partition coefficients as ways to express the distribution of a molecule between the mobile and stationary phase. Note that these equations take the form of equilibrium expressions, and that K_C is a constant for the distribution of a solute compound between two particular phases. (K_X depends on the relative volumes of the two phases.)

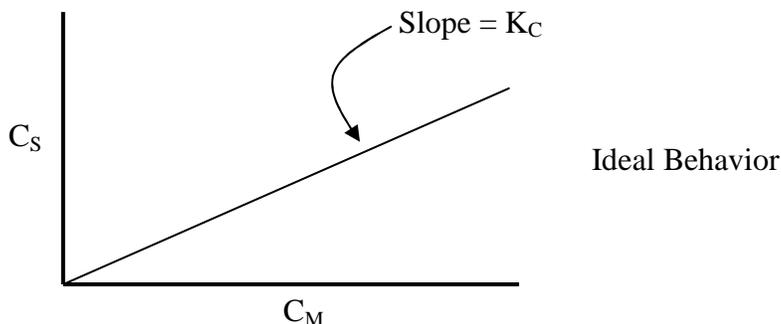
Suppose that we plotted C_S versus C_M , as shown on the coordinate system below.



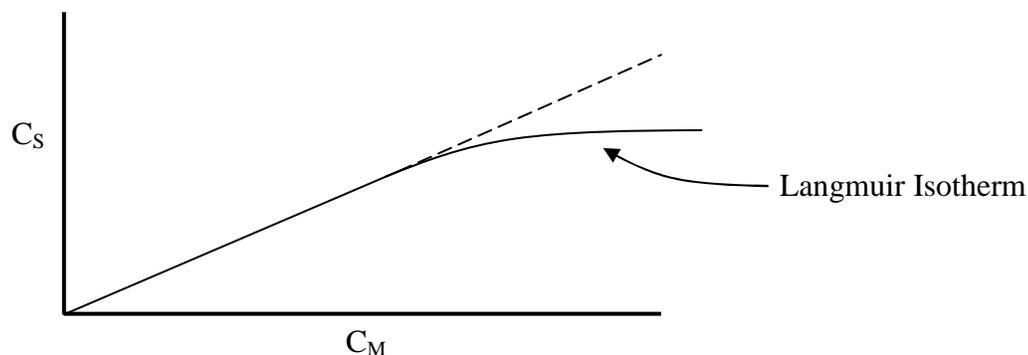
Notice that C_M plus C_S would give the total amount of the solute injected. So as you move to the right on the C_M axis, it means that more sample is being injected into the chromatograph. If we have the expression for the distribution coefficient:

$$K_C = \frac{C_S}{C_M} = \text{constant}$$

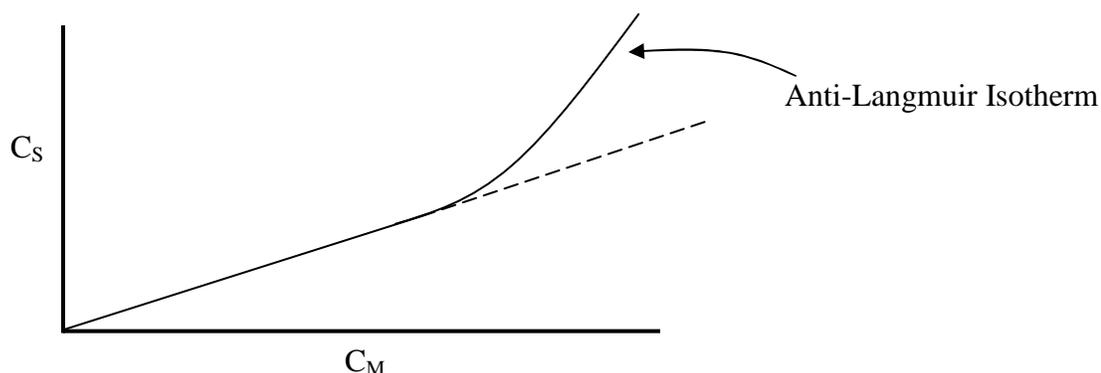
The idealized form of this plot is shown below. If we inject more sample into the column, it distributes according to a set ratio of the distribution coefficient. The result would be a straight line, with the slope being the distribution coefficient.



If we examine this in more detail, though, we will realize that the volume of stationary phase is some fixed quantity, and is usually substantially less than the volume of the mobile phase. It is possible to saturate the stationary phase with solute, such that no more can dissolve. In that case, the curve would show the behavior shown below, a result known as the **Langmuir isotherm** (Langmuir was a renowned surface scientist and a journal of the American Chemical Society on surface science is named in his honor). If we get a region of Langmuir behavior, we have saturated the stationary phase or overloaded the capacity of the column.

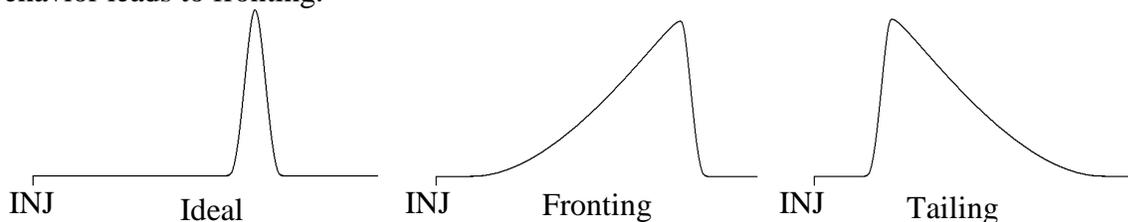


We might also ask whether you could ever get the following plot, which is called anti-Langmuir behavior.



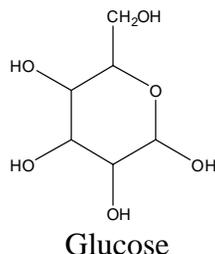
There are actually two ways this could happen. One is if the solute dissolves in the stationary phase, creating a mixed phase that then allows a higher solubility of the solute. This behavior is not commonly observed. Another way that this can occur is in gas chromatography if too large or concentrated a sample of solute is injected. At a fixed temperature, a volatile compound has a specific vapor pressure. This vapor pressure can never be exceeded. If the vapor pressure is not exceeded, all of the compound can evaporate. If too high a concentration of compound is injected such that it would exceed the vapor pressure if all evaporates, some evaporates into the gas phase but the rest remains condensed as a liquid. If this happens, it is an example of anti-Langmuir behavior because it appears as if more is in the stationary phase (the condensed droplets of sample would seem to be in the stationary phase because they are not moving).

The last question we need to consider is what these forms of non-ideal behavior would do to the shape of a chromatographic peak. From laws of diffusion, it is possible to derive that an “ideal” chromatographic peak will have a symmetrical (Gaussian) shape. A thorough analysis of this situation has been published (see Hawke). Either form of overloading will lead to asymmetry in the peaks. This can cause either **fronting** or **tailing** as shown below. The Langmuir isotherm, which results from overloading of the stationary phase, leads to peak tailing. Anti-Laugmuir behavior leads to fronting.



Adsorption Compared to Partition as a Separation Mechanism

If we go back now and consider Tswett's first separation, we see that he used solid starch as the stationary phase, and so solutes exhibited an adsorption to the surface of the starch. A useful thing to consider is the nature of the chemical groups on the surface of starch. Starch is a carbohydrate comprised of glucose units. The glucose functionality of starch is shown below, and we see that the surface is comprised of highly polar hydroxyl groups.



Silica gel (SiO_2) and alumina (Al_2O_3) were mentioned previously as two other common solid phases. If we examine the structure of silica gel, in which each silicon atom is attached to four oxygen atoms in a tetrahedral arrangement (this corresponds to two silicon atoms sharing each of the oxygen atoms), we run into a problem when you try to create a surface for this material. If we have an oxygen atom out on the edge, we would then need to attach a silicon atom, which necessitates more oxygen atoms. We end up with a dilemma in which we can never wrap all of these around on each other and only make something with the formula SiO_2 . Some of these groups are able to do this and some of the surface of silica gel consists of what are known as siloxane (Si-O-Si) groups. But many of the outer oxygen atoms cannot attach to another silicon atom and are actually hydroxyl or silanol (Si-OH) groups.



Siloxane units



Silanol units

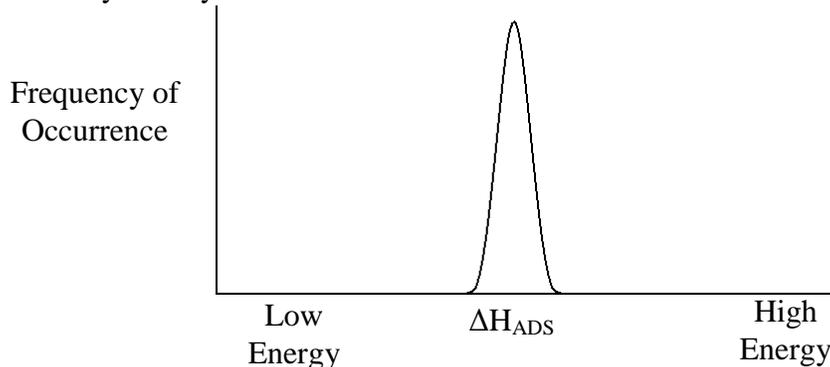
What we notice is that the surface of silica gel consists of very polar hydroxyl groups. It turns out that the same thing will occur for the surface of alumina.

If we consider a solute molecule (S), and have it adsorb to the surface of silica gel, we could write the following equation to represent the process of adsorption.

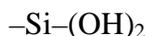
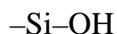


With any reaction we can talk about its enthalpy and entropy. So in this case, we could talk about the enthalpy of adsorption (ΔH_{ADS}). Suppose now we took one solute molecule and millions of surface silanols, and went through one by one and measured ΔH_{ADS} for this one solute molecule with each of these millions of surface silanols. The question is whether we would get one single ΔH_{ADS} value for each of the measurements. Hopefully it might seem intuitive to you that we would not get an identical value for each of these individual processes. Instead, it seems like what we would really get is a distribution of values. There would be one

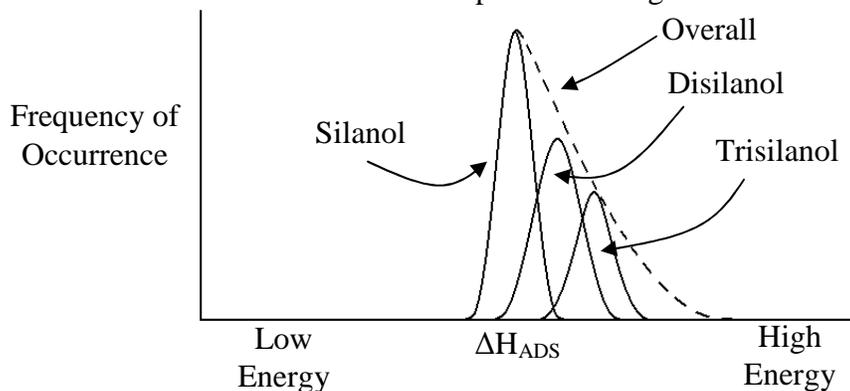
value that is most common with other less frequent values clustered around it. For some reason, some silanol sites might be a bit more active because of differences in their surrounding microenvironment, whereas others might be a bit less active. Suppose we entered all these measurements in a spreadsheet and then plotted them as a histogram with number of measurements of a particular value versus ΔH_{ADS} . But another important question involves the nature of this distribution of ΔH_{ADS} values. Would it be symmetrical as shown below, or would it have some asymmetry?



The easiest way to think of this is to examine the nature of the silanol groups on the surface of silica gel. One thing we could ask is whether there are different types of silanols, as shown below (are there also disilanols and trisilanols?).

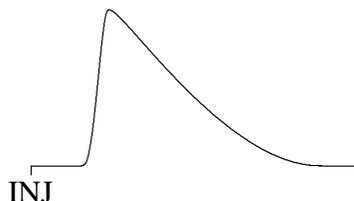


It turns out that we will get some di- and trisilanols, although these are far fewer in number than the monosilanols. It should make sense that even if the distribution about a monosilanol were symmetrical, that the di- and trisilanols will have different distributions of ΔH_{ADS} . Assuming that ΔH_{ADS} is larger for the di- and trisilanols, that might lead to the following plot for each of the individual distributions and then the composite drawing for the overall distribution.



Notice the asymmetry in this plot with a smaller number of highly active sites. Something to realize is that even if we had only monosilanols, there is still experimental data that shows a small proportion of highly active sites that produced an asymmetric distribution. It is important to realize that not everything in nature occurs in a symmetrical manner.

The key question for us to ask is what a chromatographic peak would look like for a solute traveling through this stationary phase. Hopefully it seems reasonable to predict that the peak for the solute would also be asymmetric. Those solute molecules adsorbed at the highly active sites would essentially get stuck on the column and take much longer to elute. The asymmetric peak observed in the figure below is said to exhibit tailing. Note that tailed peaks are undesirable in chromatographic separations because they are more likely to overlap with each other and interfere with the separation. Unless the solid surface is highly deactivated, all chromatographic separations based on adsorption will exhibit peak tailing. This causes an inherent inefficiency in adsorption methods.



Tailed Peak in Adsorption Chromatography

One last thing before we move on is to understand that strong adsorption by molecules on active solid surfaces has a profound implication in environmental chemistry. Consider a leaking, underground tank of gasoline at a service station. The soil around the tank gets contaminated by the leaking gas and it is desirable to clean it up. One way is to remove all the contaminated soil, heat it in a very high temperature oven that combusts all the hydrocarbon components of the gasoline, and recycle the soil. This is a common remediation procedure. But suppose the soil exists over a very large area (say the soil surrounding an old hazardous waste dump). This may be too large a volume of soil to use the removal and combustion method. The chemicals may have leached far away from the original site, contaminating nearby drinking wells.

Based on our knowledge of chromatography, and essentially using the ground as something similar to a chromatographic column, we could imagine pumping lots of clean water in from wells outside the contaminated area, and removing contaminated water from wells internal to the contaminated region. After some time of pumping, all the contaminants ought to migrate by a chromatographic-like process from the outside to the inside and be removed. If you do this, you eventually see that the level of contaminants in the water coming out of the inner wells drop considerably (maybe even to acceptable levels). But if you allow the system to sit for quite a while, you start to discover elevated levels of contaminants in the water again. What has happened is that some of the contaminants adsorbed quite strongly to the solid surfaces in the ground and were unavailable to the water. As the system sat, these slowly began to come off the surface into the water, raising the concentration. This kind of treatment process has generally proven ineffective as a way of completely treating such ground water contamination. It does get rid of a lot of the contaminants, but the strong adsorption requires enormous lengths of time before the levels would drop low enough.

Chromatographic methods languished under these inefficient methods for many years until Martin and Syngé reported the first application of a partition separation in chromatography in 1941. Recognizing that WWII was taking place in 1941, there was a considerable need for wool clothing for soldiers from England fighting in the war. Wool is rather unique as a fabric since it retains much of its warmth even if wet. In fact, so much wool was needed that England did not have enough sheep to provide the volume of wool clothing that was necessary. Martin and Syngé were interested in seeing whether it was possible to make artificial wool, and sought to examine the amino acid content of the proteins that make up wool fibers as a first step in understanding the chemical nature of wool. What they also realized, though, was that separating amino acids using adsorption chromatographic methods available at that time was going to be a difficult process. They therefore investigated whether it would be possible to take a solid particle and coat it with a liquid stationary phase, and perform the separation based on partitioning. What they found was that it was possible, and that the chromatographic efficiency was improved considerably when compared to methods based on adsorption.

The important thing to realize here is that we no longer have an adsorption process, but the dissolution of the solute into another liquid solvent. The relevant enthalpy to consider here is the enthalpy of solvation (ΔH_{SOLV}). It turns out that ΔH_{SOLV} of a particular solute in a particular solvent will also show a distribution of values; however, in this case, the distribution is a symmetrical one. Therefore, a chromatographic peak for a solute being separated entirely by a partitioning mechanism between the mobile and stationary phases ought to be symmetrical as well. This will greatly enhance the efficiency of the chromatography. This work was so important that it was recognized with the Nobel Prize in 1952. The only problem was that there were still other important issues with liquid chromatography such that it really could not flourish as an analytical method (we will examine these other issues later in our unit on chromatography).

One intriguing aspect of Martin and Syngé's 1941 paper is the last sentence, which predicted that it should be possible to use gas as the mobile phase (i.e., gas chromatography), and that some of the limitations that restrict the efficiency of liquid chromatography should not occur in gas chromatography. What was also interesting is that it was not until 1951, that James and Martin published the first report in which gas chromatography was described as an analysis method. Much of the delay was because of WWII and the need for scientists to devote their research to areas of immediate national concern related to the war effort.

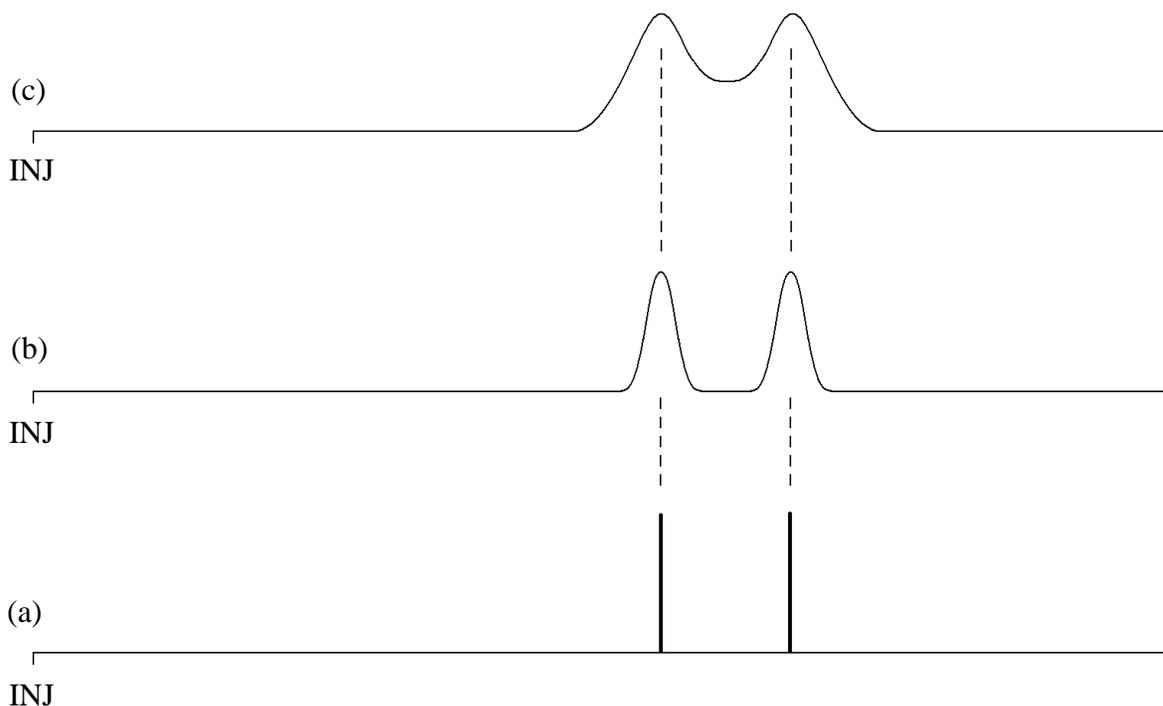
The introduction of gas chromatography revolutionized the entire field of chemical analysis. One thing, as we will develop in the next substantial portion of this unit, is that gas chromatographic methods had certain fundamental advantages over liquid chromatographic methods when it came to column efficiency. It was possible, using gas chromatography, to separate very complex mixtures of volatile chemicals in very short periods of time. Before gas chromatography, no one even considered that it might be possible to separate as many as 50 to 100 constituents of a sample in only an hour. The other thing that prompted an explosion of interest in gas chromatography as an analysis method was the development of some highly sensitive methods of detection in the 1950s and 1960s. People were now able to sense levels of molecules that were not detectable in other, conventional solution-phase systems. Part of the problem with solution-phase analysis is the overwhelming volume of solvent that can interfere with the technique used to perform the measurement. Gas phase measurements, where the

overall density of molecules is very low, do not have as much potential for interference from gases other than those being measured.

What we now need to do is develop an understanding of what created the inherent advantage in efficiency of gas chromatographic columns, and then understand what took place to improve the efficiency of liquid chromatographic columns. When we talk about the efficiency of a chromatographic column, what we really refer to is the width of the chromatographic bands of solutes as they migrate through the column.

BROADENING OF CHROMATOGRAPHIC PEAKS

One of the most important occurrences in chromatographic systems is the broadening of peaks as compounds move through the chromatographic column. For example, if we examine the figure below in which both sets of peaks have the same retention times but different extents of broadening, we see that the set of conditions that produce the narrower set of peaks (Figure b) resulted in “better” or more efficient chromatography. What we observe in the chromatogram with less peak broadening is that the peaks are more fully resolved and that we could fit more peaks into a similar window of time in the chromatogram. An ideal chromatographic system would therefore produce peaks that were straight line spikes in which no broadening occurred (Figure a).



It turns out that there are specific processes that occur in chromatographic systems that cause peaks to broaden. It also turns out that these processes are often influenced by experimental variables that we may have some control over. Contributions to broadening in chromatographic systems can be divided into two broad areas of concern. One is the contribution from what is known as **dead volume**. Dead volume refers to all the volume in a chromatographic system from the injector to the detector other than the column. Remember, the separation only occurs in the column. All other volumes (tubing used to connect components, volume within the detector cell, etc.) have the ability to contribute to peak broadening but not to the separation. One general goal then is to try to reduce the total dead volume to as small a quantity as possible. In liquid chromatography this involves using very narrow internal diameter tubing and short lengths of tubing to connect the components, using small-volume detector cells, etc. The fittings that are used to connect pieces of tubing together or components to each other have been designed specifically to reduce the dead volume to minimal levels and in ways that do not promote mixing and broadening.

The other source of broadening is within the column. If you were to examine state-of-the-art columns that are used today in gas and liquid chromatography, it turns out that there are several features of their design that lead to significant reductions in peak broadening. In other words, these columns represent the best we can do today to reduce the broadening of peaks, and therefore represent the most efficient column technology. It is worth taking the time to understand the various contributions to peak broadening that occur within the chromatographic column and to examine the ways in which current gas and liquid chromatographic columns have been designed to minimize these effects.

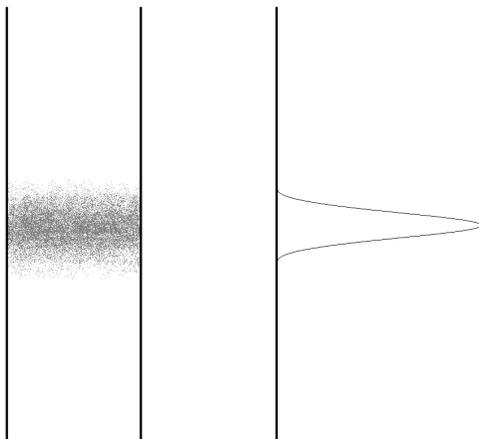
There are four general contributions to broadening within chromatographic columns. These are known as:

- longitudinal diffusion
- eddy diffusion
- mass transport broadening in the stationary phase
- mass transport broadening in the mobile phase

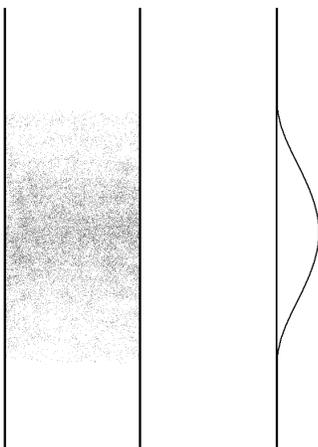
Before moving on, it is worth remembering back to two fundamental criteria we talked about with regards to chromatographic columns, the number of theoretical plates (N) and the reduced plate height (h). Remember that a column with more plates, or better yet a column with a small reduced plate height, was more efficient and provided better separations. We can therefore use the reduced plate height as a determining measure of the efficiency of a chromatographic column. **The smaller the value of h , the more efficient the column.** What we will develop as we analyze the four contributions to broadening above is an equation, which was first known as the van Deemter equation (J. J. van Deemter described the first treatment of this for chromatographic systems in 1956), that relates these four terms to the reduced plate height.

Longitudinal Diffusion Broadening in Chromatography

Consider a band of a compound in a chromatographic column. The band has the following concentration profile.



The first thing to consider is what would happen to this profile if the flow of the column was stopped and the column was allowed to sit. We know from the random process of diffusion that there is a statistical preference in which more molecules diffuse away from regions of high concentration to regions of low concentration. If we were to allow this band to sit stopped in the column, it would slowly diffuse out from its central region and lead to a broadening of the concentration profile as shown below.



This observation of diffusion from a region of high concentration to one of low concentration will occur whether the band of material is sitting stationary in a column or is flowing through the column. A molecule flowing through a column has two means of movement. One is the physical flow that is taking place. But the other is still its ability to diffuse in a random manner from one point to another. All compounds moving through a chromatographic column must exhibit some degree of longitudinal diffusion broadening. Therefore, we can never get the idealized chromatogram shown in figure (a) at the beginning of this section.

An important thing to consider is whether this phenomenon is more significant (i.e., happens faster and therefore causes more broadening, everything else being equal) in gas or liquid chromatography. To consider this, we would need to know something about the relative rates of diffusion of gases and liquids. A substance with a faster rate of diffusion will broaden more in a certain amount of time than something with a slower rate of diffusion. So the relevant question is, which diffuses faster, gases or liquids? I suspect we all know that gases diffuse appreciably faster than liquids. Just imagine yourself standing on the opposite side of a room from someone who opens a bottle of a chemical with the odor of a skunk. How fast do you smell this odor? Compare that with having the room full of water, and someone adds a drop of a colored dye to the water at one side of the room. How fast would that color make its way across the water to the other side of the room? In fact, gases have diffusion rates that are approximately 100,000 times faster than that of liquids. The potential contribution of longitudinal diffusion broadening to chromatographic peaks is much more serious in gas chromatography than in liquid chromatography. In liquid chromatography, the contribution of longitudinal diffusion broadening is so low that it's really never a significant contribution to peak broadening.

Finally, we could ask ourselves whether this phenomenon contributes more to band broadening at higher or lower flow rates. What we need to recognize is that longitudinal broadening occurs at some set rate that is only determined by the mobile phase (gas or liquid) and the particular molecule undergoing diffusion. In the gas or liquid phase, it would be reasonable to expect that a small molecule would have a faster rate of diffusion than a large molecule. If we are doing conventional gas or liquid chromatography using organic compounds with molecular weights from about 100 to 300, the differences in diffusion rates are not sufficient enough to make large differences here. If we were comparing those molecules to proteins with molecular weights of 50,000, there might be a significant difference in the rate of diffusion in the liquid phase. If the longitudinal diffusion occurs at a set, fixed rate, then the longer a compound (solute) is in the column, the more time it has to undergo longitudinal diffusion. The compound would be in the column a longer time at a slower flow rate. This allows us to say that the contribution of longitudinal diffusion to overall peak broadening will be greater the slower the flow rate. If we use the term B to represent longitudinal diffusion broadening and v to represent flow rate, and want to relate this to h , we would write the following expression:

$$h = \frac{B}{v}$$

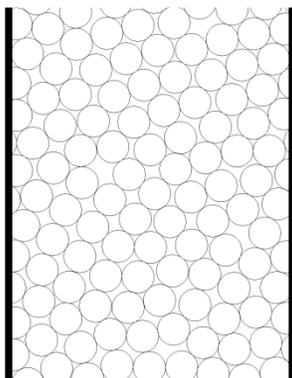
Remember that the smaller the reduced plate height the better. At high flow rates, B/v gets smaller, h is smaller, and the contribution of longitudinal diffusion to peak broadening is smaller.

We can also write the following expression for B : $B = 2\phi D_M$

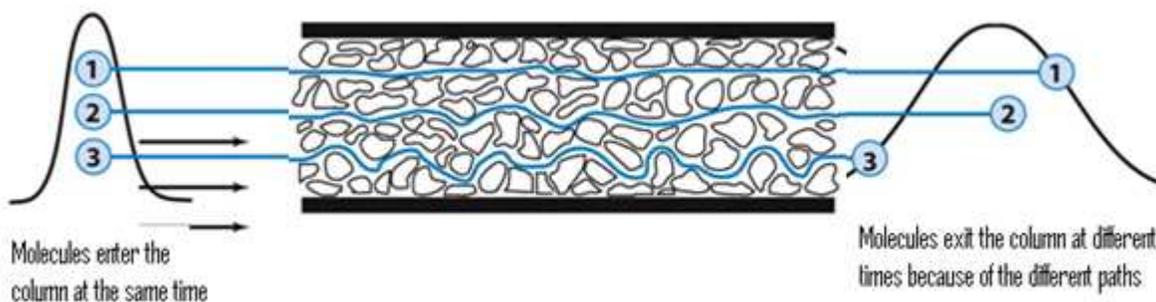
In this case, D_M refers to the diffusivity (diffusion coefficient) of the solute in the solvent. Notice that this is a direct relationship: the faster the rate of diffusion of the solute, the greater the extent of longitudinal diffusion. ϕ is known as the obstruction factor, and occurs in a packed chromatographic column. In solution, a molecule has an equal probability of diffusion in any direction. In a packed column, the solid packing material may restrict the ability of the solute to diffuse in a particular direction, thereby hindering longitudinal diffusion. This term takes this effect into account.

Eddy Diffusion (Multipath) Broadening in Chromatography

Consider a group of molecules flowing through a packed bed of particles. Another way to think of this is to imagine you and a group of friends following a river downstream in a set of inner tubes. The river has a number of rocks in the way and a variety of different flow paths through the rocks. Different people go in different channels either because they paddle over to them or get caught in different flows of the current as they bounce off of obstacles.



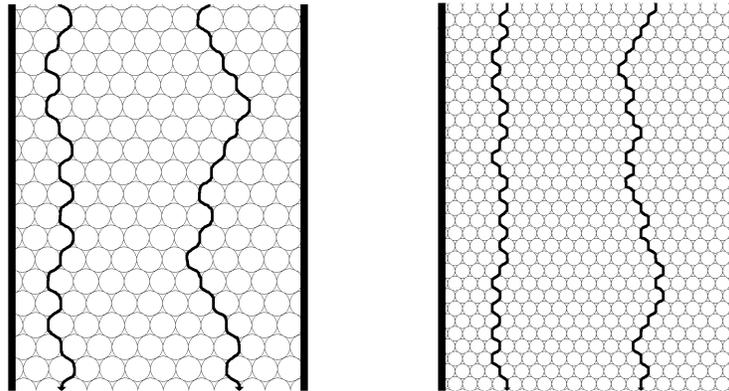
The question we need to consider is whether different molecules would have different path lengths as they passed through the bed. Would each person traveling down the river travel a slightly different distance, or would everyone travel the exact same distance? I suspect we can see that different molecules would end up traveling paths with different lengths. One molecule (Molecule 1) might find a relatively straight shot through the packed bed, whereas another might encounter more obstacles that needed to be circumvented (Molecules 2 and 3). If we watched a group of molecules pass through a packed bed, and then mapped out each path with a length of string, we would see if we then stretched out all the strings, that there was a distribution of path lengths with some being shorter and some being longer. If that were the case, the molecule with the shortest path length would move through the column more quickly (Molecule 1). The molecule with the longest path length would move through the column more slowly (Molecule 3). If we have a distinction between the times it takes a set of molecules to move through the column based only on different path lengths, we have broadened the peak. This is known as eddy diffusion.



A key factor to consider when examining eddy diffusion is to ask whether the difference in length between the shortest and longest path depends at all on the diameter of the particles. If it is, we could then ask which particles (smaller or larger) would lead to a greater difference in path length?

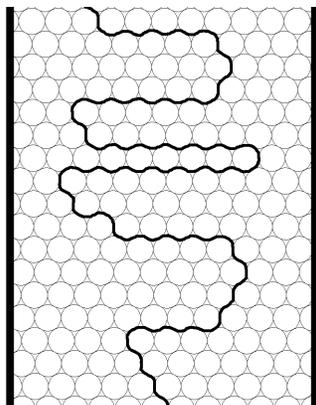
Almost everyone who is asked the first question seems to intuitively realize that the size of the particles must somehow make a difference. It just seems too coincidental to think that the difference between the shortest and longest path would be identical if the particle sizes are different. But interestingly enough, almost everyone, when they first consider this, seems to select the wrong answer when figuring out which particle (small or large) would lead to a greater difference in path length between the shortest and longest path. And remember, the important distinction is the size of the difference between the shortest and longest path, not whether one column would uniformly have longer path lengths than the other.

To help with this assessment, two columns are pictured below, one with small particles, the other with larger particles.

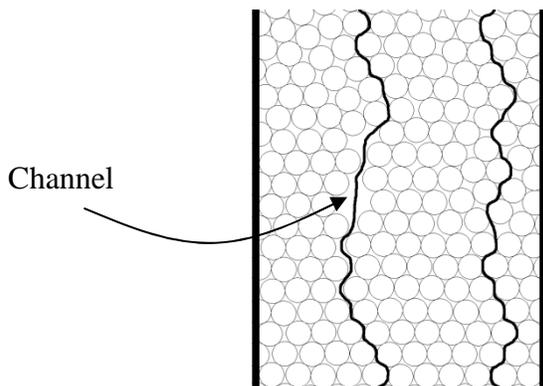


Note that the greatest distinction will occur between two molecules, one of which has found a relatively straight shot through the column, the other of which has encountered a lot of particles and so has to travel around them. Also note that the distance a molecule needs to travel around a larger particle is larger. Now you might be inclined to say that if we have to travel around lots of small particles, wouldn't that eventually add up to the larger distance of travelling around one larger particle? Turns out that it doesn't! The conclusion is that smaller particles will reduce the contribution of eddy diffusion to peak broadening (although we will add a proviso in just a bit). In other words, the distribution of path lengths of a set of molecules travelling through a packed bed is more uniform for a bed containing smaller particles than it is for a bed made up of larger particles. Thus, regarding eddy diffusion, there is a theoretical advantage to using smaller particles. That is the reason we use the reduced plate height ($h = H/d_p$) instead of the plate height for an overall assessment of column efficiency. If we had two people pack a column with the idea of seeing who packed a better one, if one person used smaller particles they would have a competitive advantage if we only compared the plate height (H).

It is also worth realizing that the flow profile shown below for a molecule would not occur (okay, there's probably some infinitesimally small possibility that this could occur, but it's so small that we could ignore it) in a chromatographic column. There is a physical flow pushing the material through the column and when a molecule reaches a flowing area, it will generally be swept downstream.



Some packed columns exhibit channeling, and channeling leads to a significant and undesirable amount of eddy diffusion. The illustration below shows a column with a channel and compares two flow paths, one of which goes through the channel.



Channels provide a straight path through a portion of the column and molecules in a channel avoid any need to move around any particles. A molecule moving through a channel will have a much more streamlined or shorter path than a molecule in an adjacent part of the column that has to move through the packed bed. Channels occur when the particles stick together in some way and separate from each other, instead of nesting in together in a packing arrangement with every particle closest together. A liquid chromatographic column that has dried out (all of the mobile phase is allowed to evaporate) will likely develop channels during the drying process that will never close back up if it is rewetted. Channels in chromatographic columns are undesirable and introduce a lot of broadening into the system.

Another key thing to ask then is whether channeling is more likely to occur with smaller or larger particles. Channeling will occur if a column is poorly packed. There are very specific procedures that have been developed for packing gas and liquid chromatographic columns that are designed to minimize the chance that channeling will occur. One key to packing a good

column is to slowly lay down a bed of particles so that they nest into each other as well as possible. In packing a gas chromatographic column, this will usually involve slowly adding the particles to the column while vibrating it so that the particles settle in together. Liquid chromatographic columns are usually packed slowly under high pressure. A column is packed efficiently when the particles are in a uniform bed with the minimum amount of voids. Given a particular particle size, the goal is to fit as many of them as possible into the column. We can then ask which is more difficult to pack efficiently, larger or smaller particles.

One way to think about this is if you were asked to fill a large box (say a refrigerator box) with basketballs or tennis balls. The goal is to fit as many of either one in as possible. You could imagine readily taking the time to carefully lay down each basketball into the refrigerator box, layer by layer, and fitting in as many basketballs as possible. You might also be able to imagine that you would start slowly with the tennis balls, laying in one in a time, and quickly lose patience at how long this would take to fill the entire box. If you then sped up, say by slowing dumping in balls from a pail while a helper shook the box, you would probably create more voids in the box. Also, because the interstitial volumes between the tennis balls will be smaller than that with the basketballs, any channels become more significant. The result is that it is more difficult to avoid the formation of channels with smaller particles. Recapping, smaller particles have a theoretical advantage over larger particles, but more care must be exercised when packing smaller particles if this theoretical advantage in column efficiency is to be realized.

Do open tubular capillary columns exhibit eddy diffusion? Capillary columns do not have packing material. Instead, they are long, narrow diameter tubes that have a coating of a liquid stationary phase on the internal walls of the column. A cartoon of a capillary column with a uniform coating of a liquid on the walls is shown below.



Because there is no packing material to move around, there would not be any eddy diffusion in such a column. The absence of eddy diffusion broadening is one advantage that capillary columns have when compared to packed columns.

Finally, we could ask whether eddy diffusion exhibits any dependence on the flow rate.

This actually turns out to be a difficult question to answer with conflicting opinions and data about whether there is a flow dependence, and if so, exactly what the dependency is. If we go back to van Deemter's initial development of peak broadening in chromatography in 1956, we would see that van Deemter believed that the contribution of eddy diffusion to peak broadening did not depend in any way on the flow rate. This is a reasonable argument if we thought that we could draw a variety of different flow paths through a packed bed, and the difference in length between the shortest and longest flow path would be fixed irrespective of how fast the molecules were moving through the path.

But let's return to our river analogy to see how the flow rate might get involved in this. Suppose the river had a relatively fast flow rate, such that different people in different inner tubes got locked into particular flow channels and stayed in those all the way down the river. Under that situation, each path would have a preset length and even if we slowed down the flow, so long as you were locked into a particular path, the difference in distance would be invariant. But suppose now we slowed down the flow so much that there were opportunities to drift around at points and sample a variety of flow paths down the river. This might lead to some averaging and the amount of sampling of different flow paths would be greater the slower the flow. This same thing can happen in a chromatographic column and leads to the conflicting data and opinions about the nature of any flow rate dependence on eddy diffusion. Also, the exact point at which there is a crossover between a rapid flow that locks in a flow path versus a slow one that allows each molecule to sample many different flow paths is impossible to determine. This point is still not fully resolved, and literature on band broadening show different terms for eddy diffusion. We usually denote eddy diffusion by the term A . If you look at van Deemter's initial treatment of peak broadening, you would see (note, van Deemter also did not use the reduced plate height, but we could write $h = A$ as well):

$$H = A$$

(where $A = 2\lambda d_p$)

Note how the particle diameter (d_p) is included in this equation for A , so that the smaller the particle diameter, the smaller the contribution of eddy diffusion to the reduced plate height.

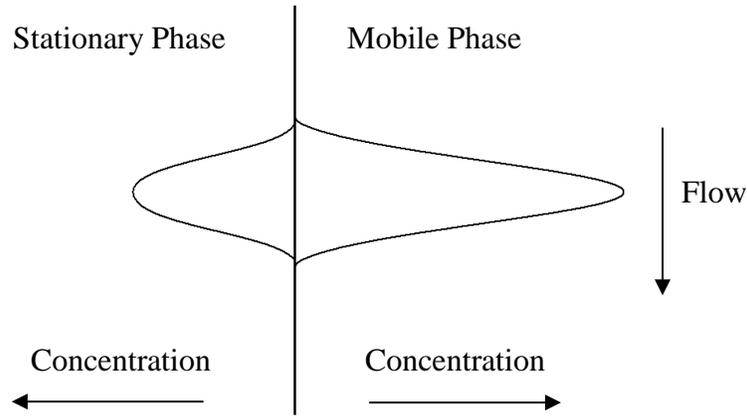
Another common conclusion today is that the contribution of eddy diffusion broadening does exhibit a slight dependence on flow rate. The usual form of this is that the dependence is $v^{1/3}$, and you might often see books or articles that include the following term in the overall band broadening equation.

$$h = A v^{1/3}$$

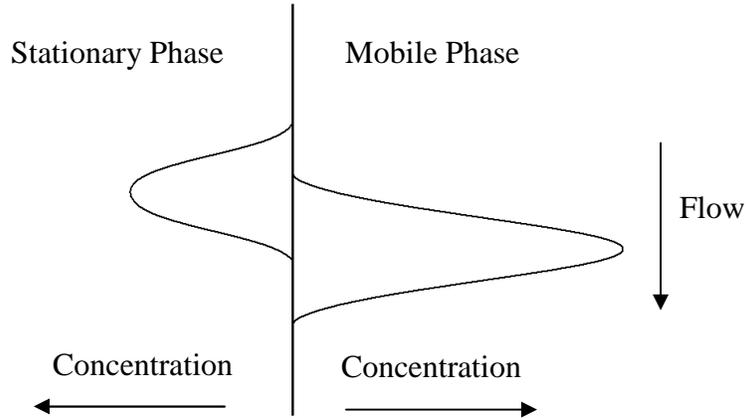
Still other people throw up their hands at all the confusion regarding eddy diffusion and show overall band broadening equations that do not have any A -term in them. We will develop another broadening term that has to do with processes going on in the mobile phase (and note that eddy diffusion only involves the mobile phase - none of what we talked about even requires the presence of a liquid stationary phase), so some people lump the eddy diffusion term into this other mobile phase term.

Stationary Phase Mass Transport Broadening

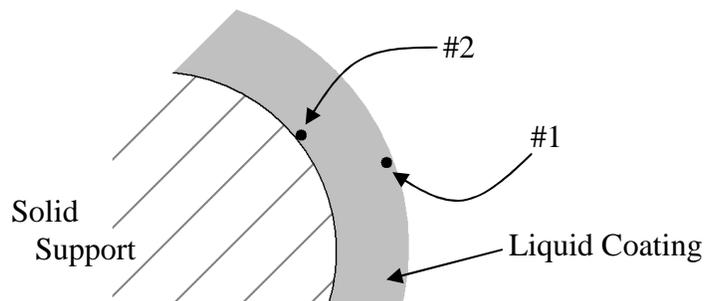
Consider a compound that has distributed between the mobile and stationary phase within a plate in a chromatographic column. The following might represent the concentration distribution profiles in the two phases (note that the compound, as depicted, has a slight preference for the mobile phase).



What we want to do is consider **what would happen to these two concentration profiles a brief instant of time later**. Since the mobile phase is mobile and the solute molecules in it are moving, we could anticipate that the profile for the mobile phase would move ahead a small amount. The figure below illustrates this.

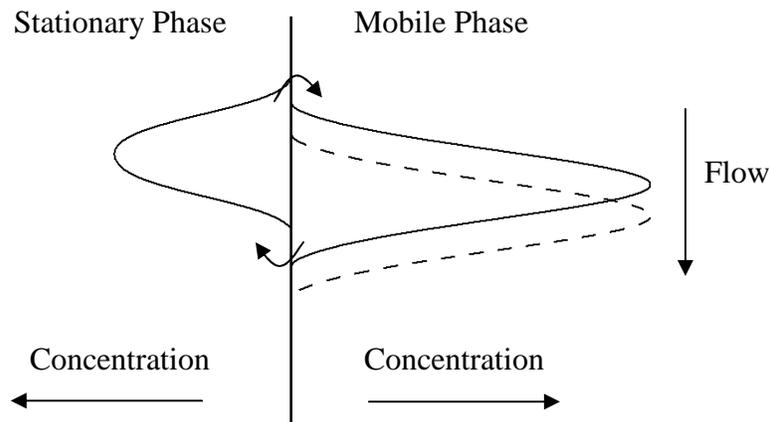


What about the concentration profile for the solute molecules in the stationary phase? Consider the picture below for two solute molecules dissolved in the stationary phase and let's assume that these are at the very trailing edge of the stationary phase distribution.



What we observe is that the molecule labeled 1 is right at the interface between the stationary and mobile phase and provided it is diffusing in the right direction, it can transfer out into the mobile phase and move along. The molecule labeled 2, however, is essentially “trapped” in the stationary phase. It cannot get out into the mobile phase until it first diffuses up to the interface. We refer to this process as mass transport. The solute molecules in the stationary phase must be transported up to the interface before they can switch phases. What we observe is that the solute molecules must spend a finite amount of time in the stationary phase. Since the mobile phase solute molecules are moving away, molecules stuck in the stationary phase lag behind and introduce a degree of broadening.

If we then consider the leading edge of the mobile phase distribution, we would observe that the molecules are encountering fresh stationary phase with no dissolved solute molecules and so these start to diffuse into the stationary phase when they encounter the surface. We can illustrate this below with arrows showing the direction of migration of solute molecules out of the stationary phase at the trailing edge and into the stationary phase at the leading edge.



Hopefully it is obvious from this picture that the finite time required for the molecules to move out of the stationary phase leads to an overall broadening of the concentration distribution and overall broadening of the peak.

A critical question to ask is whether the contribution of stationary phase mass transport broadening exhibits a dependence on the flow rate. Suppose we go back to the small amount of time in the first part above, but now double the flow rate. Comparing the first situation (solid line in the figure above) to that with double the flow rate (dashed line) leads to the two profiles. Hopefully it is apparent that the higher flow rate leads to a greater discrepancy between the mobile and stationary phase concentration distributions, which would lead to more broadening.

The term used to express mass transport broadening in the stationary phase is C_S (not to be confused with the C_S that we have been using earlier to denote the concentration of solute in the stationary phase). If we wanted to incorporate this into our overall band broadening equation, recognizing that higher flow rates lead to more mass transport broadening and reduced column efficiency (higher values of h), it would take the following form:

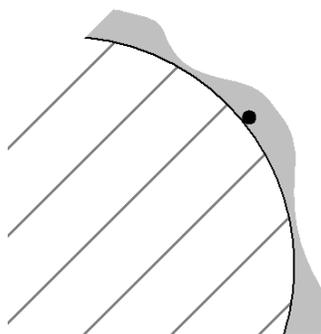
$$h = C_S v$$

Something we might ask is whether the flow rate dependency of the mass transport term has any troublesome aspects. An alternative way to phrase this question is to ask whether we would like to use slow or fast flow rates when performing chromatographic separations. The advantage of fast flow rates is that the chromatographic separation will take place in a shorter time. Since “time is money”, shorter analysis times are preferred (unless you like to read long novels, and so prefer to inject a sample and then have an hour of reading time while the compounds wend their way through the column). If you work for Wenzel Analytical, we’re going to try to perform analyses as fast as possible and maximize our throughput. The problem with speeding up the flow rate too high is that we begin to introduce large amounts of mass transport broadening. The shortening of the analysis time begins to be offset by broad peaks that are not fully separated. Ultimately, stationary phase mass transport broadening forces us to make a compromise between adequate efficiency and analysis time. You cannot optimize both at the same time.

Another thing we need to think about is what effect the thickness of the stationary phase has on the magnitude of stationary phase mass transport broadening. The picture below serves to illustrate this point.



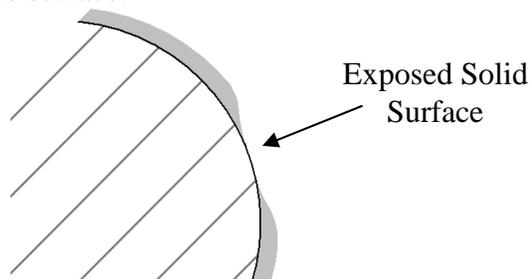
Remember that the key point is that solute molecules spend a finite amount of time in the stationary phase, and since solute molecules in the mobile phase are moving away, the longer this finite time the worse. Therefore the thicker the phase, the more broadening will occur from stationary phase mass transport processes. This says that the ideal stationary phase coating ought to be microscopically thin, so that molecules rapidly diffuse into and out of the stationary phase, thereby reducing how far ahead mobile phase molecules can move in this finite amount of time. We should also be able to realize that the optimal coated phase ought to have a uniform thickness. If we have thin and thick regions as shown below, we see that the time spent in the stationary phase by solute molecules will vary considerably, an undesirable situation.



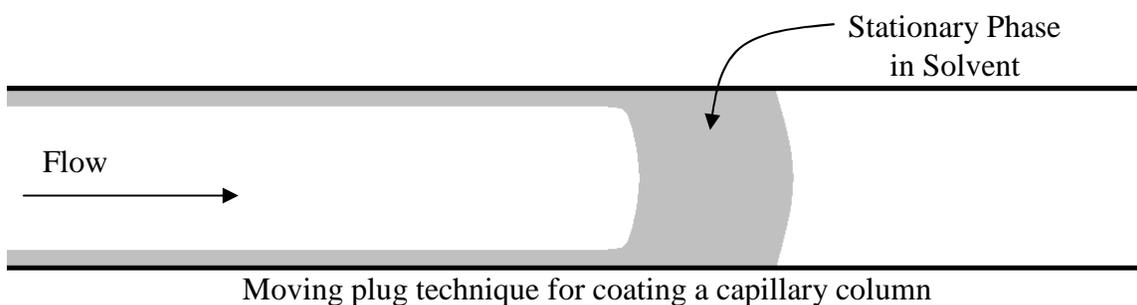
But it turns out that there are two problems with microscopically thin coated phases. If we consider the picture above, where we have two particles with the same size but different thickness coatings, a packed column with the thinner coating would have much lower capacity. For example, the phase in the middle figure on page 29 with the thicker coating might be something like a 5% weight coating of the liquid on the solid, whereas the phase with the thinner coating might be only a 1% weight coating of the liquid on the solid support. Increasing the capacity has several advantages. One is that it helps in the separation of the mixture (something we will learn more about later in the course). The other is that it is easy to overload or saturate a column that has a very low capacity.

This raises the question of whether you could design a column that had a thin stationary phase coating but the higher capacity like that in the figure on page 29 (5% loading of liquid by weight on the solid support). There is a way to accomplish this, and it involves using smaller particles. If you could imagine taking the large solid support particles in the Figure and crushing them into a bunch of smaller particles, you would realize that the smaller particles have a lot more surface area. If we then coated the same amount of stationary phase (5% by weight), because of the larger surface area, we have to get a thinner coating. So what we see again is that the use of smaller particles has a theoretical advantage over the use of larger particles.

The other problem with coating microscopically thin phases is the risk of leaving some of the surface of the solid support uncoated. These exposed solid surfaces provide highly active sites for adsorption of solute molecules, and we have already seen how adsorption is an inefficient process that leads to peak tailing. What we have then is an advantage of using small particles with thin coatings, but great care must be taken in coating these phases to ensure a complete coverage with uniform thickness of the surface.

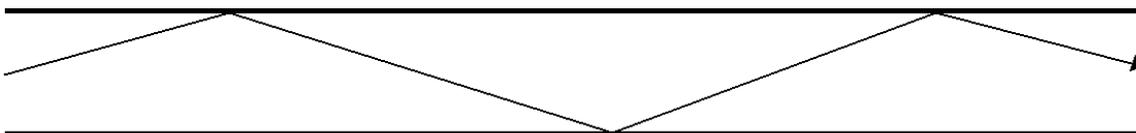


Open tubular capillary columns are common in gas chromatography. Back in the early days of capillary gas chromatographic columns, these were made of glass tubing that was approximately the same diameter as a melting point capillary that you are familiar with from organic chemistry. These columns were stretched from thick-walled glass tubes that were heated in an oven. As the capillary tube was stretched out, it was coiled in a coiling oven. It was common to use 30-meter lengths, essentially a 30-meter long glass slinky. The most common process for coating a capillary column involves what is known as the “moving plug” technique. As illustrated below, the liquid stationary phase is dissolved in a plug of solvent that is pushed through the column using pressure from an inert gas. As the plug moves, it coats a very thin layer of liquid onto the inside walls of the column. As the solvent evaporates, a very thin layer of liquid stationary phase remains on the walls of the column. A systematic process is used to treat the inside walls of the column prior to coating to ensure that the liquid wets the surface well and is deposited uniformly over all of the interior surfaces.



One problem with these glass columns was their fragility. Many frustrated workers broke the columns trying to mount them into a gas chromatograph with leak-proof fittings. The fittings used with these glass columns are usually made of graphite, a soft substance that often can be molded around the tube without breaking it (but if you're not careful, it's easy to break it). Another problem is caused by the chemical nature of glass. We think of glass as a silicate material (SiO_2), but it actually turns out that most silicate glasses contain other metal ions as constituents (aluminum, magnesium, calcium, and iron oxides are some of the other metals present). In some glasses, these other metals can be as much as 50% of the glass. These metals are positively charged centers, and if some of the surfaces are not coated by the liquid phase (an inevitable occurrence), these metal ions provide active sites for adsorption that cause tailing of compounds (especially oxygen- and nitrogen-containing compounds that have dipoles).

The capillary columns used in gas chromatography today are known as fused silica columns. Fused silica is pure silicon dioxide (SiO_2) and lacks the metal ions in regular glass. The surface of fused silica is considerably less active than the surface of regular glass. Fused silica is widely used in the production of devices known as fiber optics. Fiber optics are thin, solid glass fibers. Light is shined into one end of the fiber at an angle that causes complete internal reflection of the light as shown below.



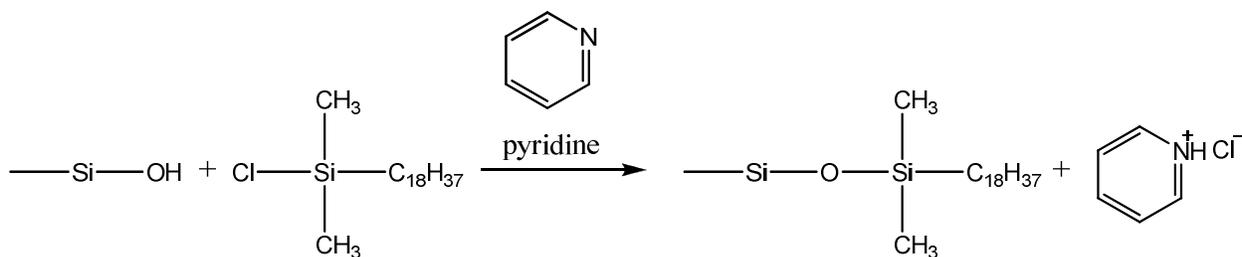
Light going in one end (say in New York City) exits out the other end (say in London, England). The light can be pulsed (sent in small bursts) and the speed of light allows for very rapid communication. It turns out to be easy to make fiber optic-like devices with a hole in the center (in fact, it took people a while to learn how to make glass fibers without the hole since the fibers tend to cool from the outside to the inside, leading to contraction and a hole in the center). The hole in the center of fused silica capillary columns is so small you cannot see it with the naked eye (we will see later that this very small opening has advantages in chromatographic applications). Also, these capillary columns are incredibly flexible. They can be tied into knots, and more importantly for chromatographic applications, leak-tight fittings can be attached without breaking the columns. The deactivated surface, flexible nature making them easy to install and use, and chromatographic efficiency (partly because of the deactivated surface, partly because of how well they can be coated, and partly because of the small diameter) make them the column of choice for most gas chromatographic applications today. The only drawback to these columns is that they have very small capacities. Gas chromatographs built to use fused silica capillary columns usually have what are known as split injection systems. A typical injection

size for a gas chromatographic sample is 1 μL . Even this amount is too much for a fused silica capillary column, but reproducibly injecting smaller volumes is very difficult. Instead, the flow from the injector is split, and only a small part (often 1 in 50 to 1 in 100) is actually sent into the capillary column. The rest is vented away and never enters the column.

Another thing we need to examine under the topic of stationary phase mass transport broadening is the nature of the stationary phase used today in liquid chromatography. In 1963, Calvin Giddings published a significant paper titled “Liquid Chromatography with Operating Conditions Analogous to Those of Gas Chromatography”. At this point in time, gas chromatography was the method of choice when performing analyses because existing gas chromatographic columns were far more efficient than the liquid chromatographic columns that were available. In fact, gas chromatography was so preferable to liquid chromatography that many publications of the 1960s and 1970s described ways of preparing volatile derivatives of non-volatile compounds so that they could be analyzed by gas chromatography. The extra steps involved in the derivatization were worthwhile since liquid chromatographic methods were not good enough to separate most compounds in complex mixtures.

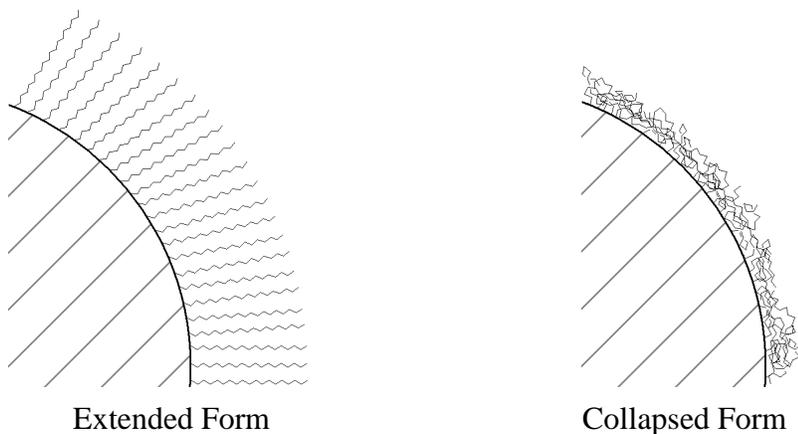
What Giddings did in this paper was show that it was theoretically possible to perform liquid chromatography at the efficiency of gas chromatography. The key feature, which we have not yet fully developed because we have one more contribution to broadening to examine, was to use exceptionally small particles with exceptionally thin coatings in liquid chromatographic columns. Of course, these exceptionally thin coatings cause several problems. One is how to coat them so that none of the surface of the solid support is exposed. If you can coat them uniformly, another problem in a liquid chromatographic system is that there might be locations in the column where the flowing liquid mobile phase can physically wash away regions of the coated phase thereby exposing the underlying solid surface. Finally, there is no such thing as two liquids that are completely immiscible in each other. It's true that oil and water don't mix, but it's also true that a little bit of oil will dissolve in water. Over time, the coated stationary phase will gradually dissolve away in the mobile phase, eventually exposing the underlying solid surface. Even though Giddings showed in 1963 how to perform liquid chromatography at the efficiency of gas chromatography, the phases that were needed could not be coated in a way that it was a widely practical method.

It was not until the late 1970s, when bonded liquid chromatographic stationary phases were introduced, that it was finally practical to do liquid chromatography with the same efficiency as gas chromatography. Bonded phases relied on silica gel, something we already encountered when we first talked about solid phase, adsorption chromatography. Silica gel is an excellent support for liquid chromatographic phases. It is physically robust, stable at pH values from about 2 to 8, and can be synthesized in a range of particle sizes including the very small particle sizes needed for liquid chromatography. The chemistry used in preparing bonded phases is shown below. Basically this involves the surface derivatization of the silanol groups on the surface of the silica gel with chlorodimethyloctadecylsilane. The C_{18} or octadecylsilane (ODS) phase shown in the scheme are the most common ones used. The pyridine is added to remove the HCl produced in the reaction.



Other common bonded phases use C₈ or C₁ surface groups. You can also purchase bonded phases with phenyl groups, C₃H₆NH₂ (aminopropyl) groups, and C₃H₆CN groups. But the C₁₈ phases are so common, and so versatile, that we will examine these in more detail.

The first thing to realize is that attaching the C₁₈ groups converts a highly polar surface (the silanol groups can form hydrogen bonds) into a non-polar surface. In effect, this is like attaching a one-molecule thick, oily skin to the surface of silica gel. There is some question about the exact conformation of the attached C₁₈ groups. Shown below are two forms, one with the C₁₈ groups extended, the other with the C₁₈ groups collapsed. There is substantial evidence to support the idea that if the non-polar C₁₈ phase is in contact with a mobile phase that is very polar (say water), that the C₁₈ groups are in the collapsed form. Putting the C₁₈ phase in contact with a less polar mobile phase (say methanol) leads to more extension of the C₁₈ groups.



It is interesting, if we examine the extended form of the C₁₈ phase, to consider the nature of this material at the outer regions. Even though the C₁₈ groups are attached to a solid, are they long enough such that the outer edges are “fluid” enough to behave more like a liquid than a solid? If so, then molecules might distribute into these phases by a partitioning mechanism. If not, then molecules adsorb to the surface. Our prior work indicated that adsorption was undesirable, but that was adsorption on a polar surface. The non-polar, deactivated nature of the C₁₈ surface does not provide strong adsorption sites so peak tailing is quite minimal.

If you look at most liquid chromatograms, though, you will see that the peaks tail more than in gas chromatography. The likely reason for this is that some of the surface silanol groups remain underivatized. Crowding of the C₁₈ groups during the derivatization process makes it unlikely that all of the silanols can be reached and deactivated. In an effort to minimize the number of

unreacted silanol groups, some commercially available C₁₈ phases are end-capped. End capping involves exhaustively reacting the C₁₈ phase with a much smaller silane such as chlorotrimethylsilane (ClSi(CH₃)₃).

Because of the covalent bonds, the C₁₈ groups cannot wash or dissolve off of the solid support. If we consider peak broadening we said, with regards to mass transport in the stationary phase, that we wanted phases as thin as possible. C₁₈ bonded phases are essentially one-molecule thick. We could never coat a one-molecule thick chromatographic phase. We could never really make a bonded liquid chromatographic phase with faster stationary phase mass transport properties.

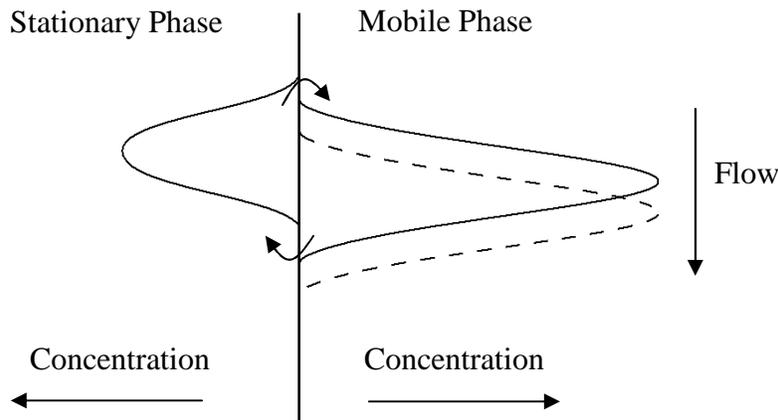
Until recently, the common particle sizes to find in commercially available C₁₈ columns have diameters of 3, 5, and 10 μm. Columns using particles of these sizes are commonly referred to as high performance liquid chromatography (HPLC). Recently columns with 1.7 or 1.8 μm particles have become commercially available and their use is referred to as ultra-high pressure liquid chromatography (UHPLC). Smaller particles will require higher pressures to force a liquid through the column and UHPLC columns can run at pressures up to 15,000 psi. In gas chromatography, we observe that the smaller particles usually have thinner coatings. Note that for these bonded phases the thickness of the phase with the 1.7, 3, 5, and 10 μm particles is always identical. What does change is the surface area. A column packed with 3 μm particles will have more surface area than a column of the same length packed with 5 or 10 μm particles. This increased surface area leads to an increase in the column's capacity. If the columns are the same length, the increased capacity will lead to increased separation of compounds and lengthen the retention times. The usual approach is to use shorter columns with the smaller particles. The shorter column reduces the analysis time because there is less volume of mobile phase in the column. Typically C₁₈ columns packed with 10 μm particles are 25 cm long; 5 μm particles are used in columns that are 15 cm long; and 3 μm particles are used in columns that are 3 cm long. These 3×3 columns can have very short analysis times. A negative aspect is that they are more susceptible to fouling by contaminants in the sample. Also, a difficulty with ultra-small particles involves packing the columns. Finally, the particles need to have uniform sizes (the smaller the particle, the smaller the tolerance on the range of particle sizes that can be used). A mixture of particles of different sizes is known as an aggregate. Concrete is an excellent example of an aggregate. The problem with an aggregate is that the smaller particles fill in the voids between the larger particles, making it very difficult to get a liquid to flow through the bed.

One last thing we could consider is whether stationary phase mass transport broadening is more significant in gas or liquid chromatography. We have to be careful here, because it's a somewhat subtle distinction. What we need to consider is the diffusion rate of the solute in the stationary phase. In gas chromatography, we have a gaseous molecule dissolved in a liquid coating. The important thing is that it is a dense liquid with a molecule dissolved in it. The diffusion rate is therefore rather comparable in this stationary phase to that of a liquid. Of course, a liquid chromatographic column is at room temperature whereas a gas chromatographic column is usually at some elevated temperature that is often higher than 100°C. We know that diffusion rates are temperature dependent, so that the rate ought to be faster in gas chromatography, and mass transport broadening in the stationary phase ought to be more significant in liquid chromatography, assuming everything else is equal. Just realize that this is not a 100,000-fold difference, because the stationary phase in gas chromatography is not a gas, but a heated liquid.

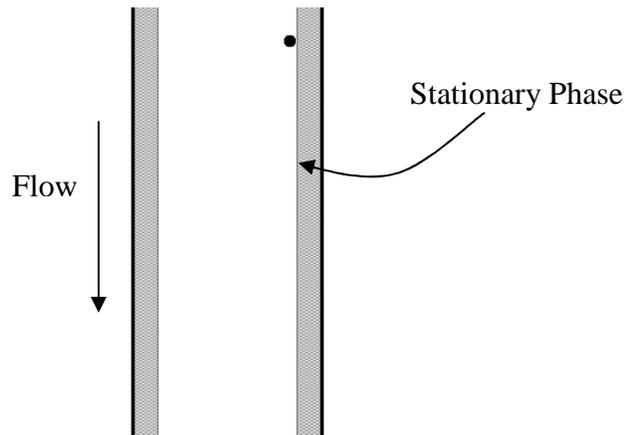
Mobile Phase Mass Transport Broadening

It's going to turn out that a similar mass transfer effect occurs within the mobile phase. The thing to consider here is that we want solute molecules to encounter the surface of the stationary phase as quickly as possible so that they can immediately undergo a distribution between the two phases.

For example, if we reconsider the picture for mass transport broadening in the stationary phase, we realize that we want the molecules at the leading edge of the mobile phase profile to quickly encounter and enter the stationary phase, otherwise they will move further ahead and broaden the distribution.

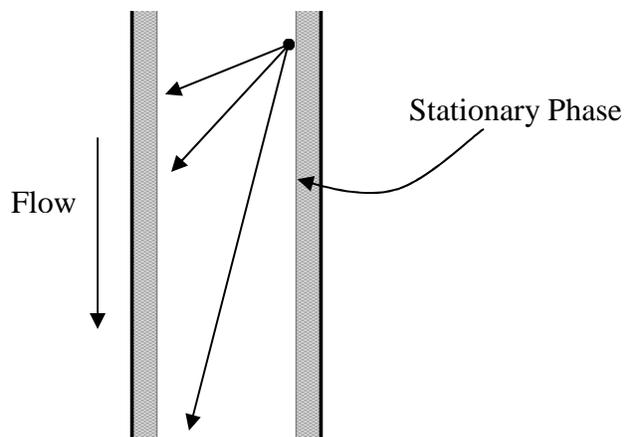


Another way to examine mobile phase mass transport broadening is to consider a capillary column as shown below.



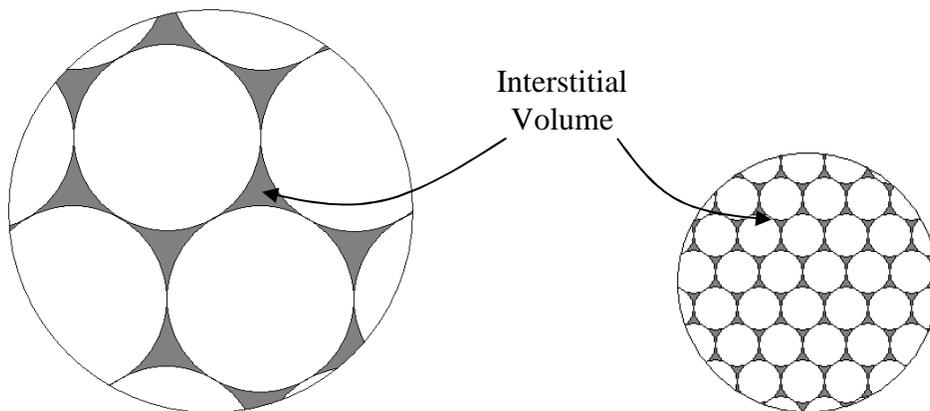
The dot represents a molecule that has just left the stationary phase and is about to diffuse across the mobile phase and re-encounter stationary phase on the other side of the column.

It is helpful to draw a line representing the path of the molecule, and then draw a second line for the path of the molecule if the flow rate were doubled. We could also imagine a situation in which the flow was so fast that the molecule never re-encountered the stationary phase. This would be a problem since it's important for the molecule to encounter the stationary phase if we are to ever have a distribution occurring that leads to a separation of two compounds.



If we are using capillary columns in a chromatographic system, what does this observation above suggest about the desirable diameter for such a column? Hopefully it would be apparent that a much smaller column diameter would lead to much faster encounters with the stationary phase. So we want capillary columns of very small diameter. That is one of the reasons why the fused silica columns used today in gas chromatography are so efficient. We can not even see the opening in these columns with the naked eye. They really approach the limit of how narrow we are able to make chromatographic capillary columns.

Next we need to ask whether this effect occurs in a packed column. If we think about a packed column, we should realize that there are voids, or interstitial volume, between the particles that make up the packing. Solute molecules need to diffuse across these voids to encounter the stationary phase. The larger the void, the more time it takes to diffuse across, and the more significant the mobile phase mass transport broadening. How can we reduce the voids? If we use smaller particles, they will pack closer together and reduce the interstitial volume between the particles. Once again, we see how small particles offer a theoretical advantage when compared to large particles. Note that this has happened in every instance when particle size made a difference. Using a packing material with smaller particles is better, provided we pack a good column with minimal to no channeling.



Another critical question to consider is whether mobile phase mass transport broadening is more significant in gas or liquid chromatography. To answer this, we need to realize that we want the solute compound to diffuse across regions of mobile phase as fast as possible. If we remember that gases diffuse about 100,000 times faster than liquids, we realize that the impact of mobile phase mass transport broadening is significantly lower for gases than it is for liquids. In fact, mobile phase mass transport broadening is the most important distinction between gas and liquid chromatography. Gases diffuse far more quickly across regions of mobile phase than do liquids. That means in liquid chromatography we need far smaller mobile phase voids to reduce the magnitude of this term. When Giddings published his important paper in 1963 on doing liquid chromatography with the efficiency of gas chromatography, this was a critical realization put forward in this paper.

What does this mean for practical applications of liquid chromatography? If we were to try to perform capillary liquid chromatography, it would mean that we ought to have columns with much smaller internal diameters than we use for gas chromatography. But gas chromatography already uses fused silica columns, which essentially reach the limit of practical internal diameters (remember, if we reduced this diameter even smaller, we introduce a problem of not having enough sample capacity in the column and would have a very difficult time actually introducing sample into the column), so capillary liquid chromatography is not a practical method and does not offer the same advantages of capillary gas chromatography. There are researchers who investigate aspects of capillary liquid chromatography, but it is not a commercial method and is not used widely by practitioners in the field. As far as packed column liquid chromatography, we have already seen how we end up using very small particles (1.7, 3, 5, and 10 μm). The real value of these small particles is that they reduce the interstitial volume of mobile phase between the particles, thereby reducing the time required for mobile phase mass transport. Gas chromatography can be done with much larger particles because of the much faster mobile phase mass transport.

The last thing we could consider about mobile phase mass transport broadening is whether its overall contribution to band broadening depends on flow rate. If we go back to our initial picture of the capillary column, we know that we want the solute molecules to encounter stationary phase as often as possible. The faster the flow, the fewer encounters, so a faster flow makes this contribution worse (this is analogous to the leading edge of the mobile phase distribution moving ahead more per unit time, thereby causing more broadening of the overall distribution). If we needed to write a term to go into our equation for h , and we represent mobile phase mass transport broadening as C_M (be careful not to confuse this with C_M the concentration of solute in the mobile phase that we have used earlier), the term would take the following form:

$$h = C_M v$$

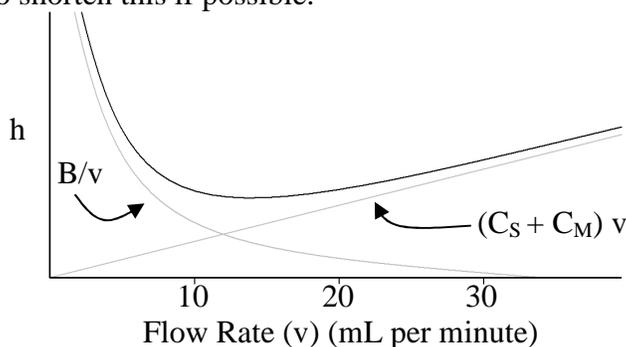
Notice how the relationship is analogous to what we saw with mass transport broadening in the stationary phase.

Concluding Comments – Peak broadening in Chromatographic Systems
Can you now draw a generalized plot of h versus flow rate?

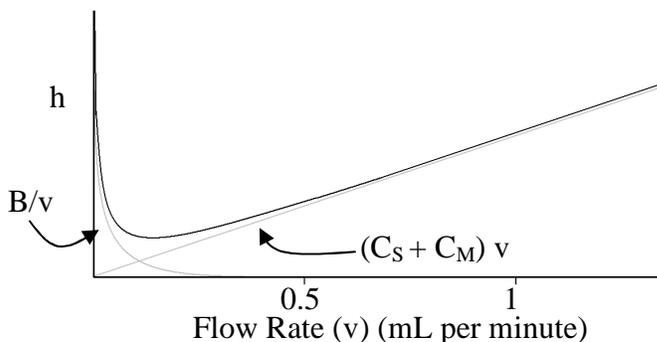
We have now developed all four contributions to peak broadening in chromatographic systems, compared their significance in gas and liquid chromatography, and seen how current state-of-the-art columns have been designed to minimize band broadening effects. We can now pull together all four of the contributions into one equation that reflects overall contributions to peak broadening. It is shown below, using one common way of expressing the eddy diffusion term:

$$h = Av^{1/3} + B/v + C_S v + C_M v$$

It is worthwhile examining the overall form of this expression. First note how the longitudinal diffusion term (B/v) will become very large at very low flow rates. Note how the mass transport terms ($C_S v$ and $C_M v$) will become very large at very high flow rates. This implies that this equation will have a minimum at some intermediate flow rate. A generalized plot of this equation for a gas chromatographic packed column is shown below. The general contributions of the longitudinal diffusion and mass transport terms to the equation are also represented. The optimal flow rate for a gas chromatographic packed column is around 15 to 20 mL/minute. A lot of times people actually run these at higher flow rates of about 30 mL/minute. The reason for this is to shorten the analysis time. Some column efficiency is sacrificed, but the entire separation process is a balance between chromatographic efficiency and analysis time, where there is a desirability to shorten this if possible.



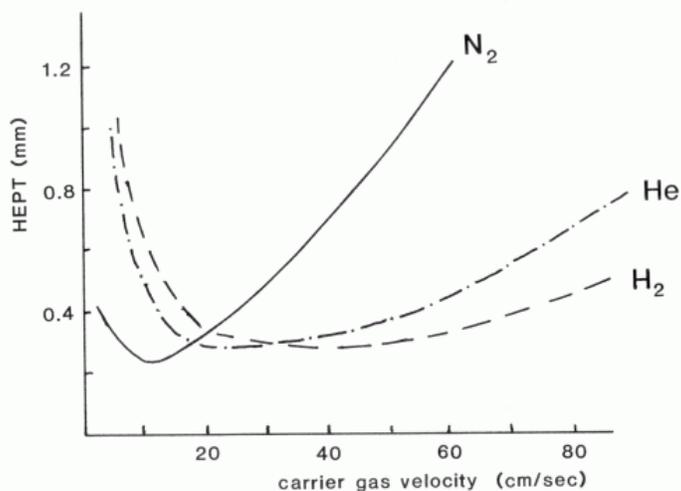
A similar plot is also shown below for liquid chromatography. Notice in this case that extremely low flow rates must be used before longitudinal diffusion becomes a significant contribution to broadening. This means that the optimal flow rate for liquid chromatographic separations is very slow, which is undesirable because of the long analysis times this would create. Instead, a common flow rate for a packed C_{18} liquid chromatographic column is in the 1.0 to 1.5 mL/minute range.



For capillary GC columns, which are more commonly used today than packed GC columns, instead of setting a column flow rate you often set the column head pressure to a value recommended by the instrument manufacturer. By adjusting the pressure of the carrier gas (usually helium) at the beginning of the column, this insures an adequate flow of gas through the column. The desired head pressure depends on the length and internal diameter of the capillary column. Longer or narrower columns will require higher pressures to maintain adequate flow. One observation is that the pressure of the gas drops from the beginning to the end of the column, such that the flow rate changes over the column as well. Instead of measuring a flow rate for a fused silica capillary column in mL/min, it is more common to measure the carrier gas velocity (u) in cm/sec. Since this value changes as well over the column, an average value is obtained by dividing the column length in cm by the retention time in seconds of an unretained compound.

$$u \text{ (cm/sec)} = \frac{\text{column length (cm)}}{\text{RT of unretained peak (sec)}}$$

A plot of the plate height versus carrier gas velocity for a column that is 25 m long and has a 0.25 mm internal diameter is shown below. The characteristic observation of an optimum velocity as which to minimize peak broadening is observed.



Why is the plot different for nitrogen versus helium as the carrier gas? The key difference between nitrogen and helium is the viscosity of the two gases. Nitrogen, as a heavier molecule, will have a higher viscosity than helium. The higher viscosity of nitrogen slows down the diffusion rates and increases the contribution of mobile phase mass transport broadening. Using helium as the carrier gas leads to improved efficiency because of the reduction in mobile phase mass transport broadening relative to nitrogen. Also, the u_{opt} for helium is at a higher flow rate meaning that the analysis time can be shortened. This plot shows that hydrogen would actually be a better carrier gas than helium. Hydrogen is rarely used as a carrier gas because of its explosion risk.

FUNDAMENTAL RESOLUTION EQUATION

Another important equation in chromatographic separations is the fundamental resolution equation. The equation relates the resolution of two compounds (R_s) to the number of theoretical plates (N), capacity factor (k'), and selectivity factor (α). Appendix I shows the derivation of the fundamental resolution equation. Since we would usually be interested in separating two compounds that are close to each other in a chromatogram, and therefore possibly not resolved, we usually think of applying this equation when we want to improve the resolution of two adjacent components.

$$R_s = \left(\frac{\sqrt{N}}{4} \right) \left(\frac{\alpha - 1}{\alpha} \right) \left(\frac{k_2'}{1 + k_2'} \right)$$

The interesting part about this equation is that it is possible to examine a chromatogram with poor resolution, decide which of the three terms is causing the most serious problem, and then make systematic experimental changes to improve the results. It is worth examining the types of experimental changes that can be made to influence each of these terms. Notice that in each case, making the term larger will improve the resolution.

N - Number of theoretical plates

One obvious way to increase the number of plates is to increase the length of the column. Doubling the length doubles the number of theoretical plates. One cautionary note about this is to consider the square root dependency on the number of plates in the equation. Doubling the column length will double the analysis time, but will not double the resolution. We would need a column four times longer to achieve a doubling of the resolution. Increasing the number of plates will always give better resolution, but there are diminishing returns when the increased analysis time is considered.

Another thing to examine is factors that influence the band broadening equation. That equation related broadening to h , and the smaller the value of h , the more plates in a column. One thing we could do is optimize the flow rate of the system. We mentioned how it was common to use a flow rate higher than the optimal one to shorten the analysis time. Slowing down the flow rate may provide enough gains in efficiency to separate two compounds that are not fully resolved.

Another change to make is to use smaller particles. In gas chromatography, this will lead to a thinner coating, improving mass transport broadening in the stationary phase. In both gas chromatography and liquid chromatography, smaller particles will reduce the interstitial volume and reduce mobile phase mass transport broadening. Smaller particles, provided they are packed well, also will reduce broadening contributions from eddy diffusion.

α - Selectivity factor

The first thing to notice about this term is that there are diminishing returns to resolution as it is made excessively large. Shown below is a chart of α and $(\alpha - 1)/\alpha$.

α	$(\alpha - 1)/\alpha$
1	0
2	$1/2$
3	$2/3$
4	$3/4$
5	$4/5$
6	$5/6$

Notice that the $(\alpha - 1)/\alpha$ term approaches a value of 1 at high values of α . Optimal α -values for most separations are between 2 and 5.

Remember that the α -value refers to the ratio of the two partition coefficients for the two components. If we wanted to make a substantive change in α , we need to change the partition coefficient of one component but not the other (or we need to change both appreciably but differently to impact the ratio). There is really only one way to do this and it involves changing the identity of the stationary phase. This would involve using a different liquid phase in gas chromatography. As we will see, there are many available liquid phases for use in gas chromatography, so changing the nature of this phase and hence the α -values is a common procedure.

In liquid chromatography, this would mean switching from a C_{18} to some other bonded phase. Since the range of bonded phases is more limited and changes of questionable utility in many instances, this is not done that frequently. One thing you might wonder about is whether changing the nature of the mobile phase in liquid chromatography would be viewed as constituting a change in α . This is easily done and is the most common way in liquid chromatography to improve the resolution of two substances that are not fully resolved. It turns out that changes to the mobile phase are generally regarded as changes to the capacity factor. Usually this might involve altering some aspect of the mobile phase so that all the compounds exhibit a higher capacity, stay on the column longer, and exhibit better resolution.

k' - Capacity factor

Similar to the α -value term in the fundamental resolution equation, the term with k' also approaches 1 at large values of k' . Therefore we can say that optimal k' values are also between 2 and 5. Also, larger k' values will always lead to longer retention and analysis times.

k'	$k_2'/(1 + k_2')$
0	0
1	$1/2$
2	$2/3$
3	$3/4$
4	$4/5$
5	$5/6$

Remember that we defined k' earlier in the course as:

$$k_2' = K_2 \left(\frac{V_S}{V_M} \right)$$

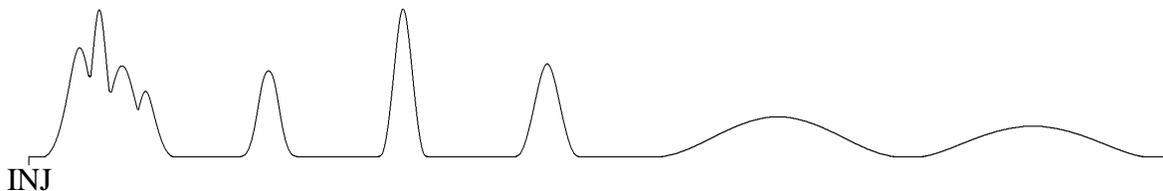
So anything that alters any of the terms of this equation will lead to a change in k' . As we already mentioned above, the most common way to change k' in liquid chromatography is to alter the constituents of the mobile phase. This will change the distribution constant (K_2), and if the correct change is made, make K_2 larger and k' larger. The analog to this in gas chromatography is to change the temperature. Recall that:

$$K_2 = \frac{C_S}{C_M}$$

We could consider what happens to this ratio as the temperature is changed. The stationary phase is a liquid. The mobile phase is a gas. Hotter temperatures reduce the solubility of a gas in a liquid (warm soda will go flatter faster). Thermal pollution refers to the reduction in the concentration of dissolved oxygen gas when warm water from a power plant or industrial cooling process is added to a river or lake. So hotter temperatures will reduce C_S , reduce K_2 and reduce k' . This would actually make the resolution worse. So by cooling down a gas chromatographic column, we increase the capacity factor and improve the resolution. Of course, this also lengthens the analysis time, which may be undesirable.

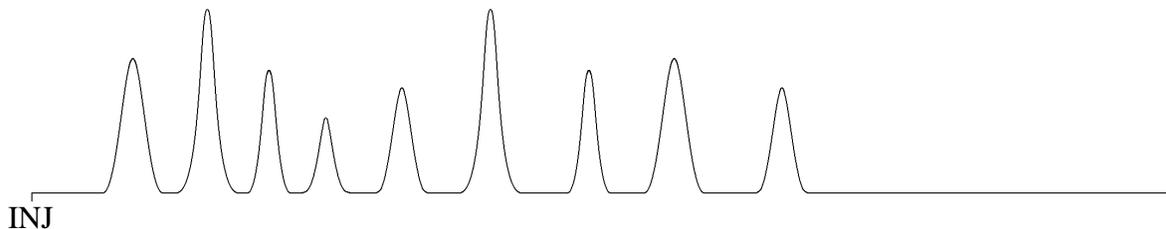
If we examine the volume terms, we realize that it is difficult to change V_M , the volume of the mobile phase. V_M is the interstitial volume and is essentially fixed for a particular particle size. There is no way to crunch the particles closer together to reduce V_M . In gas chromatography, it is easy to alter V_S , the volume of the stationary phase. This would involve coating a thicker loading (e.g., instead of 3% liquid coating, raise it to 5%). Changing V_S in liquid chromatography really is not an option since we have bonded C_{18} groups and do not coat different thickness phases. If we change the particle size from 5 μm to 3 μm , and keep everything else, we do create more capacity in the column (because the 3 μm particles have more surface area), but we create more plates as well.

Consider the following chromatogram. We observe two problems with this separation. The first few compounds come out of the column very quickly and are not fully resolved. The latter compounds are fully resolved but stay in the column too long and are very broad.



What problem exists in this separation? If we were to enlarge N to improve the resolution of the first few compounds, we would lengthen the retention time of the latter ones as well, which would be unacceptable. If we changed α , it might resolve some of the overlapped constituents but might cause some that are already resolved to now overlap with each other. We have a capacity problem (k') in this chromatogram. The first few compounds do not have enough capacity and would benefit by spending more time in the stationary phase. The latter few have too high a capacity factor and are spending too much time in the stationary phase. What we say is that a chromatogram has a limited peak capacity. In other words, it is only possible to separate a certain amount of compounds within a fixed period of time in the chromatogram. There is only some number of peaks that can be fit in side by side before they start to overlap with each other.

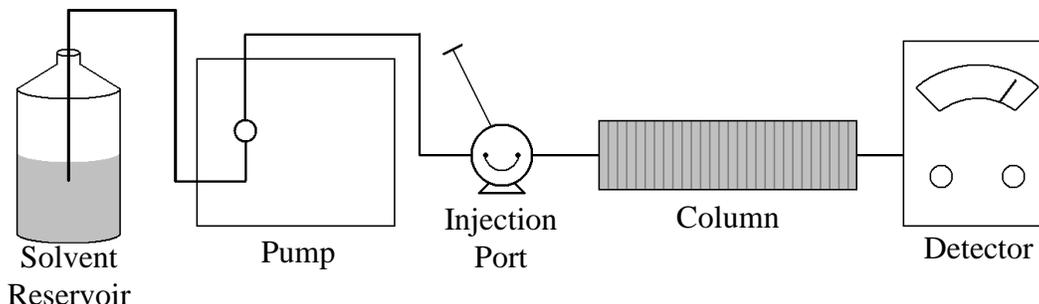
In gas chromatography, there is a way to address these problems during the chromatogram so that all of the constituents are chromatographed at a k' value that is more optimal. If we lowered the temperature during the early portion of the chromatogram, we would raise the capacity factor of these constituents of the sample and they would stay on the column longer. If we raised the temperature during the latter portion of the chromatogram, we would lower the capacity factor of these constituents and they would come off of the column faster. This systematic raise in temperature during the chromatogram is known as a temperature program. Most gas chromatograms are obtained using temperature programming rather than isothermal conditions. The temperature program chromatogram for the same mixture is shown below.



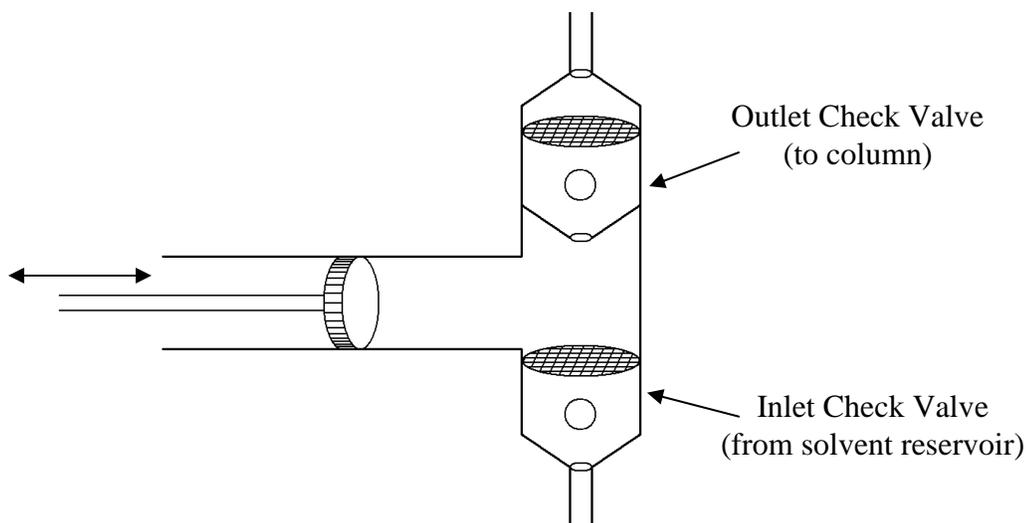
There is an analogous procedure in liquid chromatography that is known as gradient elution. In this technique, you start with a mobile phase that causes the constituents of the sample to have a high capacity factor and then systematically vary the mobile phase during the run to lower the capacity of the constituents. The exact nature of the changes that might be made to accomplish this will be discussed later in our unit.

LIQUID CHROMATOGRAPHIC SEPARATION METHODS

Liquid chromatographs are fairly simple pieces of equipment. There is a solvent reservoir that holds the mobile phase, a high pressure pump, an injection valve, a column, and a detector.

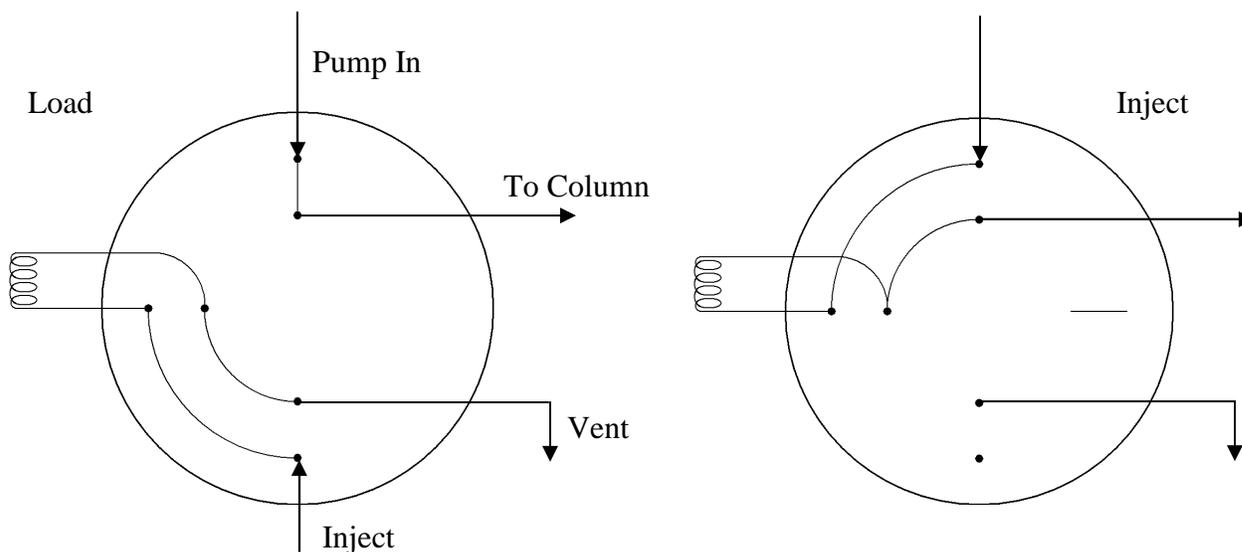


The **pumps** are usually reciprocating small volume pumps that use inlet and outlet check valves. There is a small cylinder with a sapphire piston. The inlet and outlet valves essentially have a moveable ball in them. When the cylinder is full of fluid and pushing it into the chromatograph, notice how the ball in the inlet check valve will move down and block the opening to the solvent reservoir. Also notice how the ball in the outlet check valve will pop up, allowing flow into the column. When the cylinder is almost empty and the piston recycles to fill (this recycle step is very fast), the ball in the inlet check valve pops up and allows flow from the solvent reservoir to the cylinder. The ball in the outlet check valve moves down, blocking the hole, and prohibiting flow back from the column. The flow out of a reciprocating small volume pump such as this is pulsed (when the piston recycles to fill, flow is stopped). Many liquid chromatographs employ some form of a pulse-dampening device to reduce these pulses.



The **injection valve** is usually a six-port, two-way valve with a sample loop. In one position (the load position), the flow comes in from the pump through one port and goes out another port to the column. The other two ports connect the syringe adapter to a sample loop and a vent. A common sample loop size is 20 μL . Usually you inject about 100 μL of sample into the loop. The first 80 μL cleans the loop and goes out the vent. The last 20 μL are retained in the loop and ready for injection in the system.

In the second position (the inject position), the flow from the pump now goes through the sample loop and then to the column. Moving the valve to this position allows the mobile phase to sweep the sample into the column for analysis.

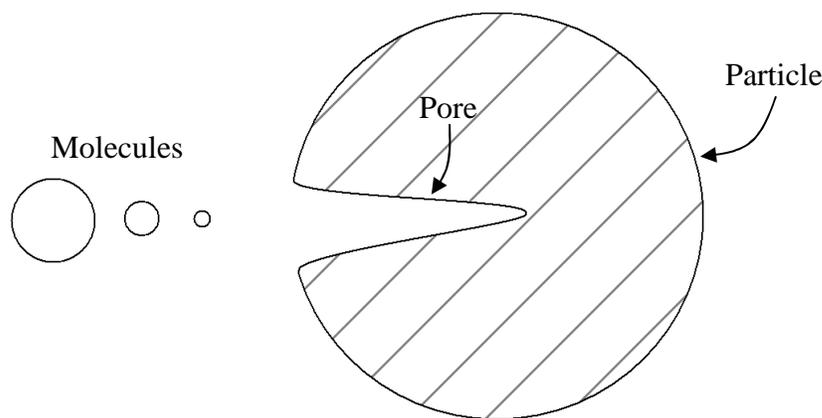


We have already discussed most of the important features of liquid chromatographic **columns**. The column lengths are usually 3, 15, or 25 cm depending on the particle size used. The internal diameter of conventional liquid chromatographic columns is 4.5 mm (about $\frac{1}{4}$ inch).

Many methods have been used for **detection** in liquid chromatography. The most common detection method is to use ultraviolet absorption. Fluorescence spectroscopy is also used for certain classes of compounds. More recently people have figured out ways to adapt mass spectrometers to liquid chromatographs. The large volume of solvent in liquid chromatography is incompatible with conventional mass spectrometric methods, so these techniques are quite specialized. Also, micro columns with smaller diameters and less solvent are often used with liquid chromatographic-mass spectrometers. One advantage of mass spectrometry over most other detection methods is that the mass spectrum provides information that may allow you to identify the chemical structure of an eluting compound.

Steric Exclusion Chromatography

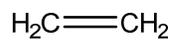
Steric exclusion chromatography is a technique that separates compounds solely on the basis of size. In order for the results of steric exclusion separations to be meaningful, there can be no directed forces between the compounds being separated and the surface of the particles used as the stationary phase. Instead, the particles are prepared with well-characterized pore sizes. Below is a cartoon of a particle with one pore in it. Also in the cartoon are representations for several molecules of different size (note, the pore size and molecule size are not representative of the scale that would exist in real steric exclusion phases – the pore is bigger than would actually occur and the molecules would never have sizes on the order of that of the particle).



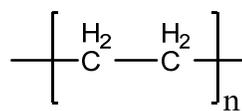
The smallest molecule is small enough to fit entirely into all regions of the pore. The largest molecule is too big to fit into the pore. The intermediate sized one can only sample some of the pore volume. Provided these molecules have no interaction with the surface of the particle and are only separated on the basis of how much of the pore volume they can sample, the largest molecule would elute first from the column and the smallest one last.

Suppose we took a molecule that was even larger than the biggest one in the picture above. Note that it would not fit into any of the pores either, and would elute with the biggest in the picture. If we wanted to separate these large species, we would need a particle with even larger pores. Similarly, if we took a smaller molecule than the smallest pictured above, it would sample all of the pore volume and elute with the smallest one pictured above. To separate these two compounds, we would need particles with smaller pores.

Steric exclusion chromatography requires large compounds, and is not generally effective on things with molecular weights of less than 1000. It is commonly used in biochemistry for the separation of proteins and nucleic acids. It is also used for separation or characterization purposes in polymer chemistry (a polymer is a large compound prepared from repeating monomeric units – polyethylene is a long, linear polymer made of repeating ethylene units).



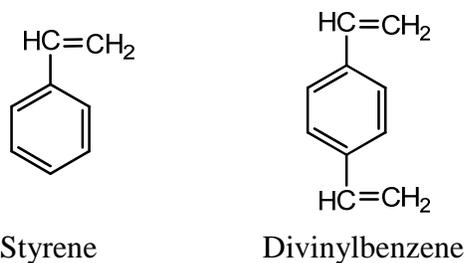
ethylene



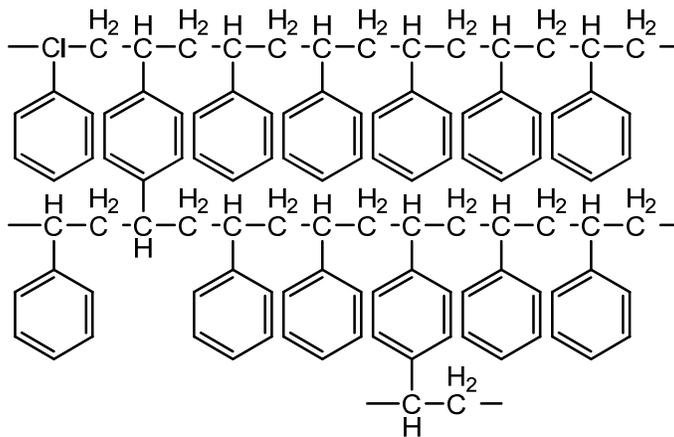
polyethylene

One critical question is how to remove the possibility of an attractive force between the compounds being separated and the surface of the porous particles. The way this is done is to use a particle with very different properties than the compound being separated, and to use a solvent that the solutes are very soluble in. For example, if we want to separate proteins or nucleic acids, which are polar and very soluble in water, we would need to use porous particles made from an organic material that had a relatively non-polar surface. If we wanted to separate polyethylenes of different chain lengths, which are non-polar, we would dissolve the polyethylene in a non-polar organic solvent and use porous particles made from a material that had a highly polar surface. This might involve the use of a polydextran (carbohydrate), which has hydroxyl groups on the surface of the pores.

The classic organic polymer that has been used to prepare porous particles for the steric exclusion separation of water-soluble polymers is a co-polymer of styrene and divinylbenzene.



If we just had styrene, and conducted a polymerization, we would get a long, single-bonded chain of carbon atoms with phenyl rings attached to it. Linear polystyrenes are soluble in certain non-polar organic solvents. The divinylbenzene acts as a cross-linking agent that bridges individual styrene chains. A typical ratio of styrene to divinylbenzene is 12:1. The cross-linking serves to make the polymer into particles rather than linear chains. The cross-linked polymer is an insoluble material with a very high molecular weight. By controlling the reaction conditions including the amount of cross-linker and rate of reaction, it is possible to make polystyrenes with a range of pore sizes.



If we think about what is inside the column, there are four important volume terms to consider. One is the total volume of the column (V_T). The second is the interstitial volume between the particles (V_I). The third is the volume of all of the pores (V_P). The last one is the actual volume occupied by the mass of the material that makes up the particles.

It turns out that V_I is usually about 0.3 of V_T for a column. There is simply no way to crunch the particles closer together to reduce this term appreciably.

$$V_I = 0.3 V_T$$

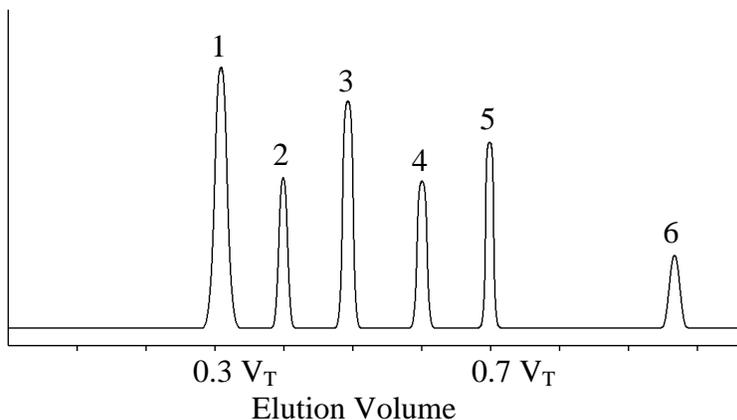
It turns out that the maximum pore volume that can be achieved is about 0.4 of V_T . If you make this larger, the particles have more pores than structure, become excessively fragile, and get crushed as you try to push a liquid mobile phase through the column.

$$V_P = 0.4 V_T$$

Totaling this up, we can write that:

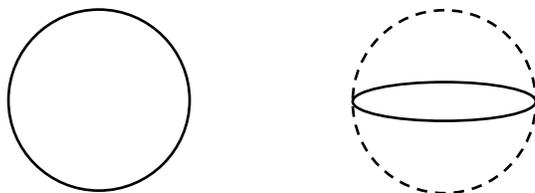
$$V_I + V_P = 0.7 V_T$$

Since there are no directed forces in a steric exclusion column, this means that all of the separation must happen in one column volume, or in $0.7 V_T$. If we then showed a chromatogram for a series of compounds being separated on a steric exclusion, it might look like that shown below.

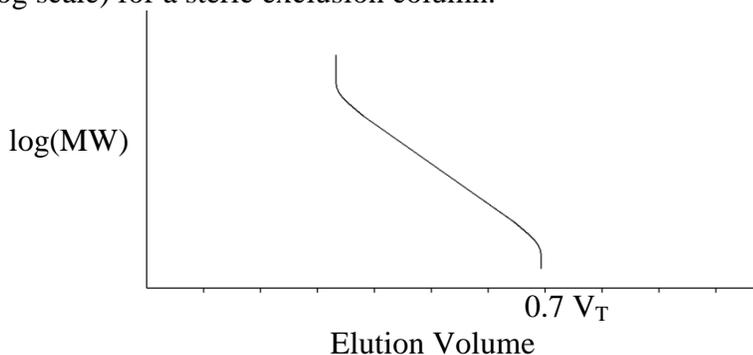


The peak labeled 1, which has the shortest retention time ($0.3 V_T$), corresponds to all molecules in the sample that had a size that was too large to fit into the pores. It cannot be known whether this is one compound or a mixture of large compounds. The peak labeled 5, which has the longest retention time ($0.7 V_T$), corresponds to all molecules in the sample that had a size small enough to sample all of the pore volume. It cannot be known whether it is one compound or a mixture of two or more small compounds. The peaks labeled 2 through 4 sample some of the pore volume depending on their size. The peak labeled 6 elutes with a retention volume that is greater than $0.7 V_T$. How would we explain the elution volume of this peak? The only way we can do so is if there are attractive forces between this molecule and the surface of the particles. This is a serious problem and we would need to examine this system and eliminate the cause of this attractive force.

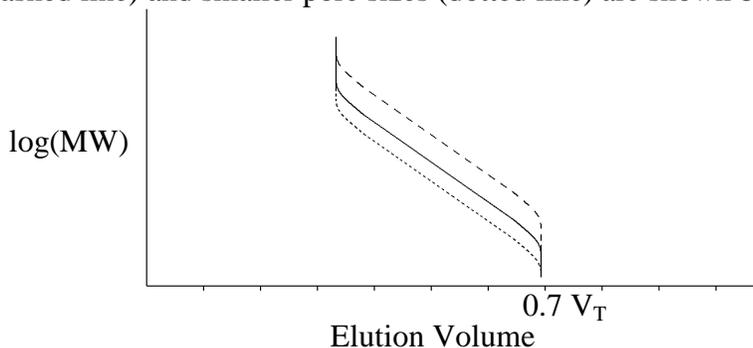
Note that this method separates things on the basis of their size. What people try to do when using steric exclusion chromatography is equate size with molecular weight. The two representations for the shape of a molecule shown below point out a potential problem with equating size with molecular weight. One molecule is spherical. The other is rod shaped. The spherical molecule probably has a larger molecular weight, because it does occupy more volume. However, the size of a molecule is determined by what is known as its hydrodynamic radius. This is the volume that the molecule sweeps out in space as it tumbles. If you took the rod shaped molecule below and allowed it to tumble, you would see that its size is essentially comparable to that of the spherical molecule.



When performing steric exclusion chromatography, you need to use a series of molecular weight standards. It is essential that these standards approximate the molecular features and shapes of the molecules you are analyzing. If you are analyzing proteins, you need to use proteins as standards. The same would apply to nucleic acids, or to particular organic polymers. Shown below is the typical outcome of the calibration of elution time with molecular weight (always plotted on a log scale) for a steric exclusion column.



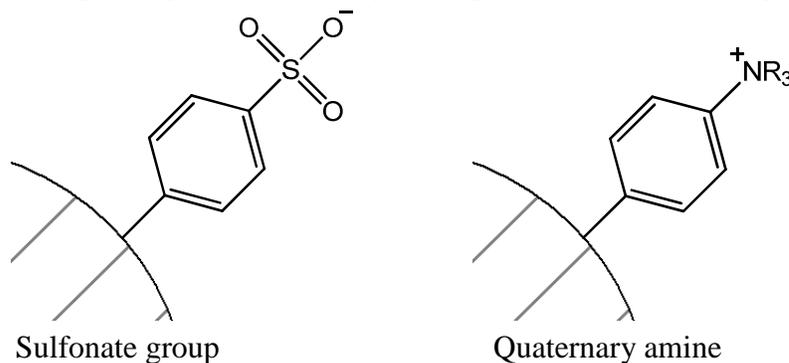
Note that excessively large molecules never enter the pores and elute together at $0.3 V_T$. Excessively small molecules sample all of the pore volume and elute at $0.7 V_T$. There is then some range of size (or molecular weight) where the compounds sample some of the pore volume and elute at volumes between 0.3 and $0.7 V_T$. The plots that would occur for particles with the next larger (dashed line) and smaller pore sizes (dotted line) are shown below.



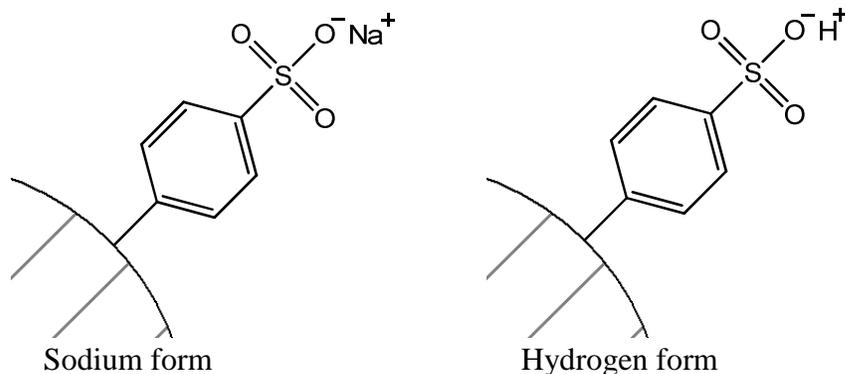
Ion-Exchange Chromatography

A second sub-category of liquid chromatography is known as ion-exchange chromatography. This technique is used to analyze ionic substances. It is often used for inorganic anions (e.g., chloride, nitrate, and sulfate) and inorganic cations (e.g., lithium, sodium, and potassium). It can also be used for organic ions, although this is less common with the advent of reversed phase liquid chromatographic methods that will be described later. Another significant application of ion-exchange chromatography is as a step in the purification of proteins. Some of the substituent groups of amino acids are charged (the total charge for a particular protein is a function of the pH of the solution), which makes ion exchange a suitable method for protein purification.

The approach is to attach fixed ionic groups to the surface of a solid support. One common support used in the formation of ion exchange resins is polystyrene-divinylbenzene copolymers. The fixed ions are attached through a derivatization of the phenyl rings of the polystyrene. Common fixed ions involve either sulfonate groups or quaternary amines. The aromatic sulfonate groups are strong enough acids that they are deprotonated at all but highly acidic pH values ($\text{pH} < 1$).

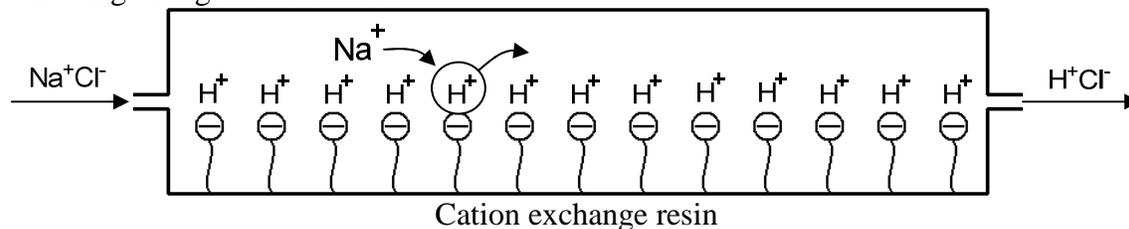


Since we must preserve neutrality in such a system, there must also be an exchangeable counterion associated with each of these fixed groups. In the case of the sulfonate group, the counterion is a cation and this is a **cation exchange resin**. With the quaternary amine phases, the exchangeable counterion is an anion and this is an **anion exchange resin**. These counterions can be exchanged with each other. For example, this would enable you to have a cation exchange resin in the sodium form or the hydrogen form.

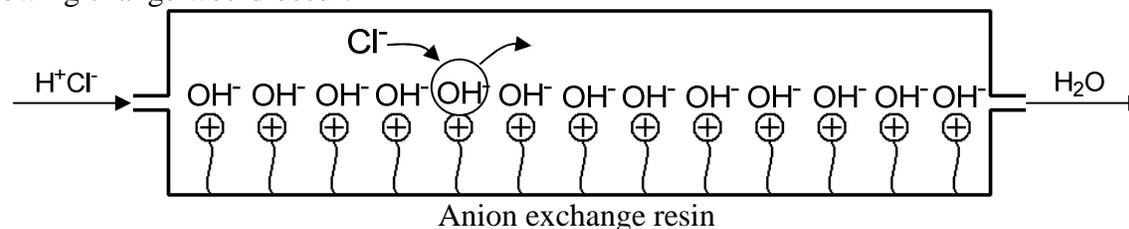


An anion exchange resin could be in the hydroxide form (OH^-) or chloride form (Cl^-).

One common use of ion exchange resins is in the deionization of water. It is useful to consider a scheme using ion exchange resins that would enable you to deionize water. If for example, we had water with sodium chloride in it (Na^+Cl^-), we would need a way of removing both cations and anions. If we first passed the water through a cation exchange resin in the hydrogen form, the following change would occur:



If we then passed the water through an anion exchange resin in the hydroxide form, the following change would occur.

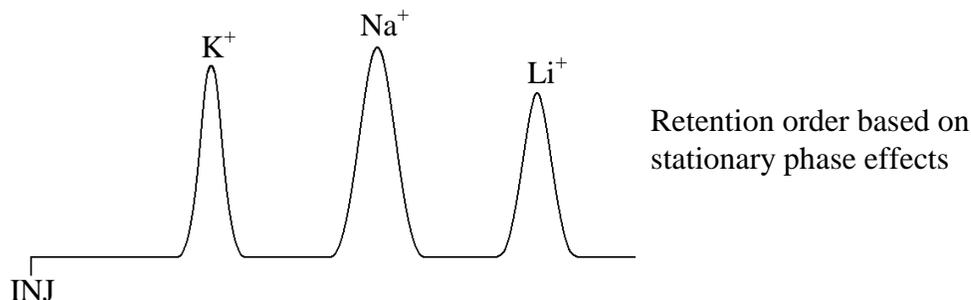


The H^+ and OH^- given off by the two resins would combine to form water. Eventually the resin will fill up with impurity ions (Na^+ and Cl^- in this case), and we would either need to replace the resin or reactivate it. We can reactivate the cation exchange resin by passing relatively concentrated hydrochloric acid through it to remove all the Na^+ and replace it with H^+ . We can reactivate the anion exchange resin by passing a relatively concentrated solution of sodium hydroxide through it to remove all the Cl^- and replace it with OH^- . To minimize how often we need to replace these resins or how frequently we need to recharge them, it's best to have resins with as high an ion exchange capacity as possible (the capacity is determined by the number of phenyl rings that have been derivatized with fixed ions).

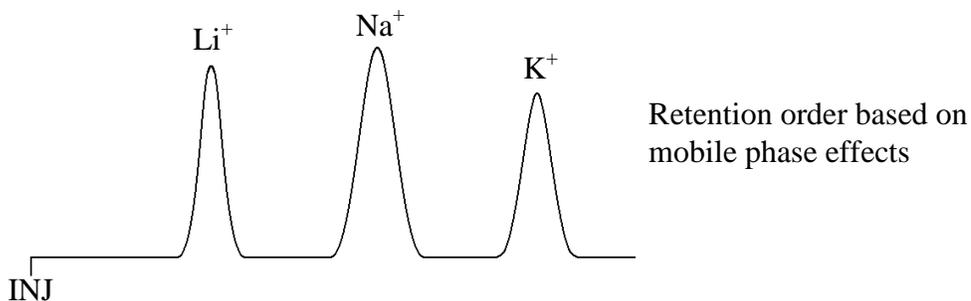
The capacity of ion exchange resins used for deionizing water is too high for analytical purposes. Presumably, the concentrations of ions in samples that we want to analyze are relatively low. If we use high capacity resins, the retention times will be much too long. One of the early impediments to the use of ion exchange as an analytical method was the lack of methods to reproducibly synthesize resins with low capacities. One of the first groups of people to figure out a way to do this was chemists at Dow Chemical. They were motivated by a need to measure inorganic anions and cations at low levels and realized that ion-exchange chromatography would be an ideal method for doing so.

With any chromatographic method, it helps to know some basic rules for predicting retention order. **An interesting example to consider in ion-exchange chromatography is the retention order for the ions Li^+ , Na^+ , and K^+ on a cation exchange resin.** One thing we can consider is whether these ions have different strength interactions with the fixed anion in the resin. All three ions have the same charge. What should also be apparent is that lithium is the smallest ion with the densest charge, potassium the largest with the most diffuse or fluffiest charge. We therefore

might predict that the attraction of the lithium ion for the sulfonate groups in the resin is the strongest of the three ions. It turns out that the equation for ionic attraction has a distance term in it, and the closer the ions, the stronger the attraction. Lithium being the smallest is effectively closer to the sulfonate and has the strongest attractive force of the three for the resin. This would suggest a retention order with potassium eluting first, sodium second, and lithium last.

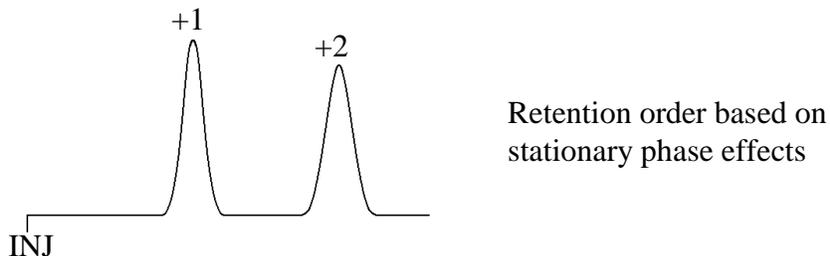


But there is also a mobile phase in chromatographic separations, and it is useful to examine whether these ions have different relative stabilities in the mobile phase. If one of the three is most stable in the mobile phase, it might be expected to stay in the mobile phase more than the others and elute first. What might affect the stability of these ions in the mobile phase? The mobile phase in this separation would be an aqueous phase. If we consider water, we know that it is unusual in having a very elaborate network of hydrogen bonds. Any ion that dissolves in water will cause some disruption of this network. The question to consider is which ion would be the most disruptive of the three to the hydrogen bond network? Since the charges of these three ions are identical, this decision will be based on the size. The larger potassium ion will be more disruptive of the hydrogen bonds, and more difficult for water to accommodate. You could then say that Li^+ is more stable in the water, stays in the mobile phase more, and elutes first. You could phrase this another way by saying that the K^+ is least stable in the aqueous mobile phase, and so is “forced” into the resin by the mobile phase and elutes last. Sometimes the chromatographic literature refers to this as the solvophobic effect. The K^+ fears the solvent and so spends more time in the resin. The relative retention order based on mobile phase effects would be lithium first and potassium last, the exact opposite of what was predicted above based on stationary phase effects.

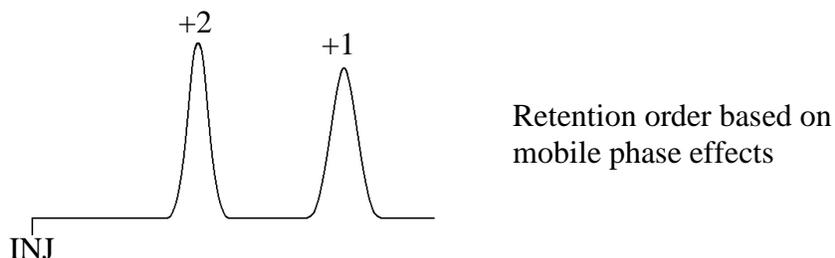


With conflicting predictions, the only way to know which one is more important is to inject the ions and determine the retention order. **In this case, the measurements show that the Li^+ elutes first and the K^+ elutes last.** The mobile phase effects are more significant in determining the retention order.

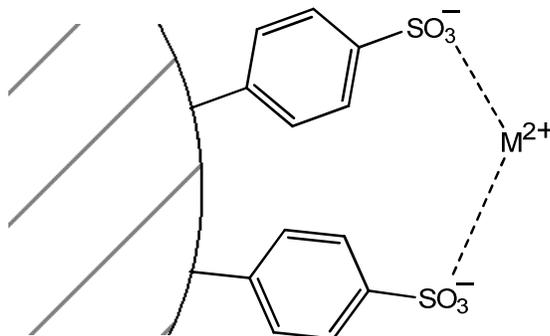
Now suppose we had two ions with exactly the same size, but one had a charge of 1+ and the other a charge of 2+. Examining stationary phase effects, the equation that describes the attraction between two ions has the charges of both ions in it. The greater the charge of the ions, the greater the attraction. We would therefore expect the 2+ ion to show greater attraction for the fixed sulfonate anions and elute later than the 1+ ion.



Examining mobile phase effects, both ions would have a similar extent of disruption of the hydrogen bond network since both have the same size. What we then need to consider is the strength of the attraction between the positive ion and the sphere of water molecules that surround it (remember, these cations would be surrounded by the slightly negative oxygen atoms of water molecules). This represents an electrostatic attraction, and again is dependent on charge. Therefore the 2+ ion is more stable in the water and ought to elute first, the exact opposite of what was predicted based on stationary phase effects.



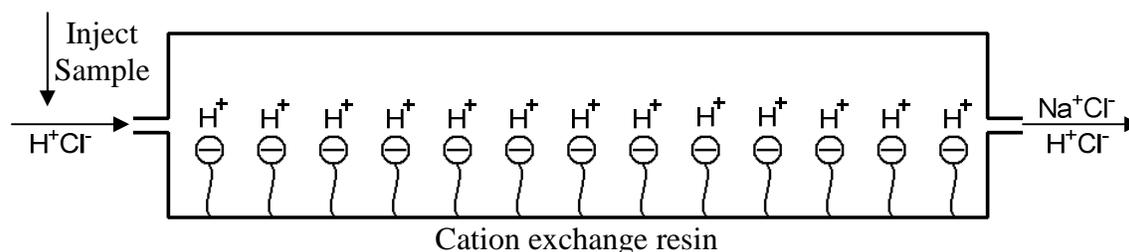
Faced with conflicting predictions, it's necessary to perform the experiment and see which comes out first. **In this case, the measurements show that the 1+ ion elutes first, the 2+ ion elutes second.** The stationary phase effects are more important in this case in determining the retention order. The likely reason why the stationary phase effects are more significant is that the 2+ ion can actually bind simultaneously at two adjacent sulfonate sites.



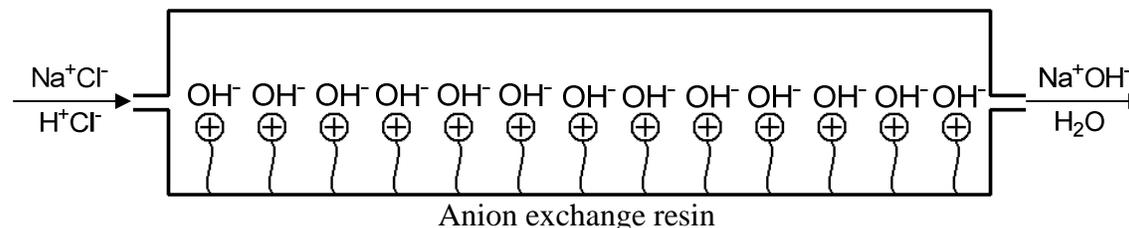
The likelihood that this occurs can be observed if a lanthanide(III) ion is added to these resins. In this case, the resin particles actually shrink in size as the lanthanide ion is added. The reason for the compression is that the binding of three sulfonate groups to the lanthanide causes the polymer to collapse in a bit to fit these groups around the lanthanide.

The separation of Li^+ , Na^+ , and K^+ described in the prior problem would often be done on a polystyrene resin using a fairly dilute solution of hydrochloric acid (perhaps 0.1 M) as the mobile phase. The bound ions would be sulfonate groups and the mobile counter ion would be the H^+ ion. An important issue is how to detect these ions. They do not absorb ultraviolet or visible light in the accessible portion of the spectrum. They do not absorb infrared light. Conductivity is one possibility for performing the measurement. The conductivity of a solution is a measure of the extent to which the solution conducts electricity. Dissolved ions are needed for a solution to conduct electricity, and the higher the concentration of ions, the higher the conductivity. We can measure the conductivity of a solution quite sensitively. In fact, this is the reading that is performed on water that has been purified by passage through a MilliQ water purification device to see just how well the water has been deionized. The only problem with trying to apply a direct conductimetric measurement is that the hydrochloric acid in the mobile phase produces too high a background signal. The chemists at Dow who had developed low capacity ion exchange resins recognized this problem as well and devised an ingenious way to remove the conductivity of the eluent ions (HCl) but retain the conductivity of the alkali ions they wanted to detect.

What they did was use a device called a **suppressor column**. If we imagine measuring Na^+ in a solution containing sodium chloride (Na^+Cl^-), we first start with a cation exchange resin in the H^+ form and would have the following eluting out the end of the column when the sodium comes off:



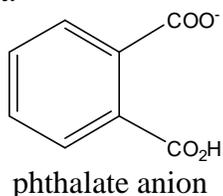
Note that there is still a high concentration of HCl mixed with the NaCl as it elutes from the column. This HCl will interfere with the measurement of conductivity. Suppose we took the column eluent and then passed it through an anion exchange resin in the hydroxide form. The Cl^- ion of the Na^+Cl^- would exchange with the hydroxide, converting this into sodium hydroxide (Na^+OH^-), a conducting electrolyte because it stays ionized. The Cl^- ion of the HCl would exchange with the hydroxide, converting this into H^+ and OH^- , which is non-conducting water. We can therefore measure a conductivity that only relates to the amount of sodium ion in the original sample. An analogous scheme, which had the columns reversed, could be used to measure the conductivity of anions that were separated on an anion exchange column in the hydroxide form.



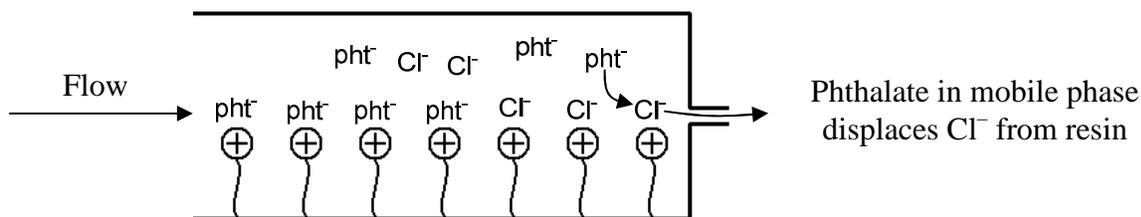
Eventually, the hydroxide counterions in the suppressor column will all become replaced with chloride ions and the device would not work anymore. The suppressor column must be periodically regenerated in the hydroxide form.

Today, instead of using suppressor columns to remove the conductivity of the eluent ions, membrane-based electrolytic neutralization devices are employed. The electrolysis of water can be used to generate hydronium and hydroxide ions, and by proper design, the desired ion can be generated in such a way to pass through a membrane and suppress the conductivity of the eluent ions. In some instruments, similar electrolytic strategies are used prior to the analytical column to generate the eluent ions as well. The use of this eluent generation technology leads to less background conductivity and better sensitivity, making it especially useful for the analysis of low levels of ions.

One other way of detecting the ions, and especially anions, was also developed by the chemists at Dow. It involved the use of **indirect spectrophotometric detection**. In this procedure, an anion such as the phthalate anion is used as the counterion in the mobile phase. The material is usually added as potassium phthalate, and maintained at a concentration of 0.001 M. The phthalate ion absorbs ultraviolet light. The background measurement in the system then consists of a high absorption reading of UV light.



Suppose we were separating Cl^- in a sample containing sodium chloride. Drawn below is the very end of the column with the chloride ions in the resin, just about to elute in the column. At this point, the concentration of phthalate ion leaving the column is 0.001 M. But what happens when a chloride ion is displaced from the resin to exit the column? This will only happen if a phthalate ion replaces it in the resin. The replacement that occurs will cause the concentration of phthalate ion to drop below 0.001 M.

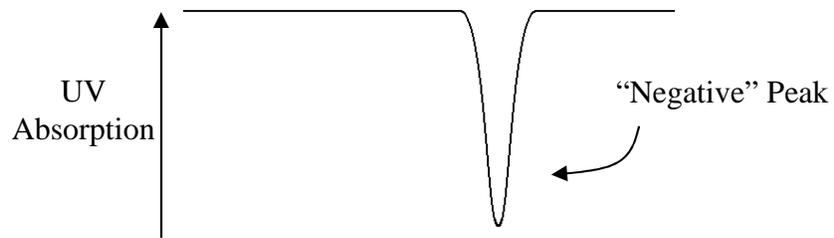


In other words, when the chloride elutes from the column, what you observe in the mobile phase is that the total concentration of anions equals 0.001 M (this has to happen in order to preserve neutrality in the system).

$$[\text{Cl}^-] + [\text{pht}^-] = 0.001 \text{ M}$$

If the concentration of phthalate ion drops proportionally to the concentration of chloride eluting from the column, the UV absorption drops proportionally as well, as shown below. The name

indirect spectrophotometric detection is aptly chosen since the value of the UV absorption drops as analyte anions elute from the column.



The people at Dow Chemical who developed the ion exchange methods for some analyses they needed to perform realized that there were others who would want to be able to measure the same species, and that the device has commercial potential. A company called Dionex, which is still the leading vendor of ion chromatographs, was created to market their invention.

Bonded-phase Liquid Chromatography

In our development of band broadening, we talked extensively about the C_{18} columns that are the most common in use today. We already mentioned that less common bonded phases including those with C_8 , C_1 , aminopropyl ($C_3H_6NH_2$) and cyanopropyl (C_3H_6CN) groups are also commercially available. Prior to the introduction of the C_{18} columns, the **normal** way to do liquid chromatography involved the use of a polar stationary phase like silica gel and a non-polar mobile phase. When the C_{18} columns were first reported, they constituted a non-polar stationary phase, and so a polar mobile phase could be employed. Since this configuration of polarities of the phases was the **reverse** of what was normally done, the use of C_{18} columns became known as **reversed-phase** liquid chromatography. Even though today almost everyone uses these reversed-phase methods, the name has stuck.

We have already seen how the deactivation of the surface with the C_{18} groups has a very positive effect on the chromatographic efficiency. Another significant advantage of using C_{18} stationary phases is that aqueous-based mobile phases are used with them. Water is the ideal mobile phase for liquid chromatography because so many substances are soluble in water. Water is the solvent of the environment. Water is the primary solvent of living systems. Many pharmaceutical agents need to possess water solubility to enter the body. Since many organic compounds are not that soluble in water, organic pharmaceuticals that are not water-soluble usually have ionic groups incorporated into them to render them water-soluble.

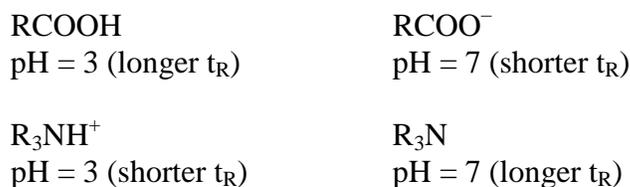
It's rare to use only water as the mobile phase with a C_{18} column. Instead, an organic modifier (methanol, acetonitrile, and tetrahydrofuran are the three most common) is added in some amount to the mobile phase. Compared to water, the chemical properties of the organic modifier are more like that of the C_{18} phase. The presence of the organic modifier therefore shortens the retention time compared to a mobile phase that was only water. Raising the concentration of the organic modifier will further shorten the retention time of almost all compounds. We mentioned the concept of a gradient elution earlier in the unit when we discussed the problem of having a limited peak capacity in a chromatogram. Remember the goal was to start with a high capacity factor and systematically change the system so that the capacity factor got shorter as the chromatogram progressed. One possible gradient procedure might be to start with a mobile phase that is 80:20 water-methanol and gradually change it to 20:80 water-methanol during the chromatogram. The increased concentration of methanol will reduce the capacity factor of the later eluting components.

Experimentally, it is easy to carry out a gradient. Using two pump heads, one pumps the initial phase and the other the final phase. A special mixing chamber exists to adequately mix the output from the two pumps. During the chromatogram, a computer systematically slows down the pump rate of the initial phase and ramps up the pump rate of the final phase.

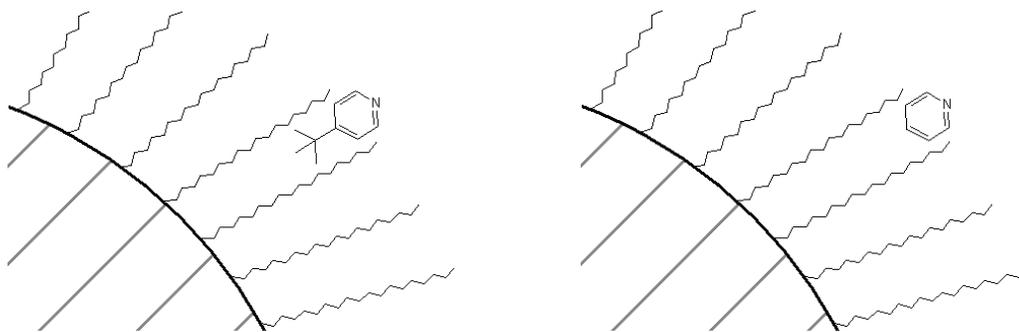
Another important variable with an aqueous mobile phase is the pH of the system. C_{18} silica gel phases are stable over the range of 2 to 8 (although 3 to 7 really represents a safer window). If the pH is too acidic, the surface C_{18} groups will be hydrolyzed off. If the pH is too basic, the silica gel itself will decompose. This pH range is one that can be used to change the nature of many acids and bases. For example, carboxylic acids at pH 3 might mostly be in their

protonated (neutral) form, whereas at pH 7 they are likely to be in their deprotonated (anionic) form. Since we would expect the neutral form to have more solubility in a C_{18} phase than the anionic form, the retention time for most carboxylic acids would be longer at pH 3 than at pH 7. If we consider nitrogen bases, we note that at pH 3 they are likely to be in their protonated (cationic) form, whereas at pH 7 they are likely to be in their deprotonated (neutral) form. Organic bases therefore would have a longer retention time at pH 7 than at pH 3. You might also recollect how we used a similar process to distinguish acids and bases in an acid/base/neutral extraction procedure discussed at the beginning of this unit. This is the same behavior and rationale going in liquid chromatography. Another gradient procedure that could be used to advantage in liquid chromatography is a pH gradient.

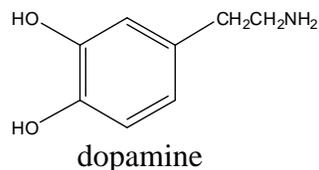
There is some debate in the literature on liquid chromatography about the exact nature of the separation procedure (adsorption on a deactive surface versus partitioning), and whether stationary phase or mobile phase (solvophobic) effects are most important in determining retention properties. It actually turns out that either one usually leads to the same conclusion as to retention order, and for our purposes, thinking about which compound of a pair has a greater attraction for the stationary phase is sufficient to predict which will come out first and which second. We have already examined the two pairs below as a function of pH.



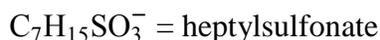
How about a comparison of the retention order of pyridine and *tert*-butylpyridine on a reversed-phase column? If you thought that the presence of the *tert*-butyl group on the pyridine would make that compound more attractive to the C_{18} groups, thereby causing it to have the longer retention time of the two, you are correct. In fact, in all likelihood, there is some preference of the association of these two compounds with a C_{18} phase as shown below. The non-polar portion of the molecule is likely oriented toward the C_{18} phase, whereas the polar nitrogen atom is oriented toward the mobile phase.



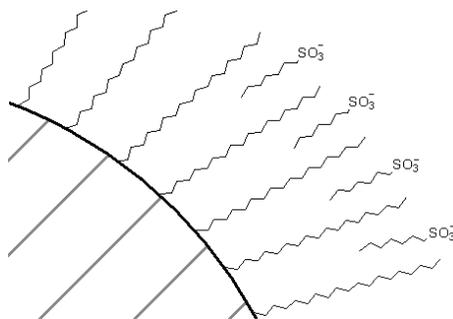
And lastly, picking up on another technique we learned with regards to liquid-liquid extractions, we could ask how we might lengthen the retention time of organic cations on a C₁₈ column. For example, there are a series of neurotransmitters such as dopamine that are based on aromatic amine derivatives.



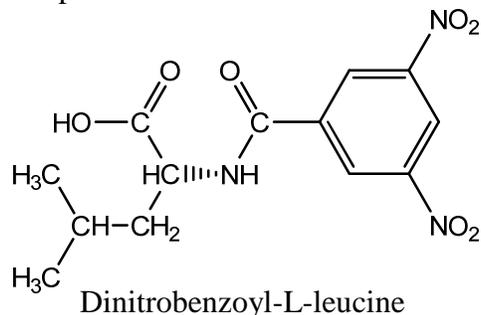
Dopamine and other similar derivatives may well be protonated under the separation conditions, and because of the protonation, have short retention times that do not facilitate the separation of the similar analogues. Can you think of a way to lengthen the retention time that does not involve adjustment of the pH? A way to do this is to add a “greasy” anion such as heptylsulfonate to the mobile phase (note, since this is added to the mobile phase the anion is continuously pumped through the system).



One way to think of this is that, just like in liquid-liquid extraction, the sulfonate anion can form an ion pair with the cation and the ion pair would have more solubility in a C₁₈ phase than the cation by itself. An alternative way to view this is that some of the sulfonate salt distributes into the C₁₈ phase as shown below. This serves to create a pseudo ion exchange material that the organic cations are attracted to. Detailed studies have shown that the latter mechanism (pseudo ion exchange resin) is the one that actually operates.



One other important category of bonded phases involves the attachment of optically pure groups to silica gel. The compound dinitrobenzoyl-L-leucine is one example of such a phase. These types of phases are used for the separation of enantiomers.



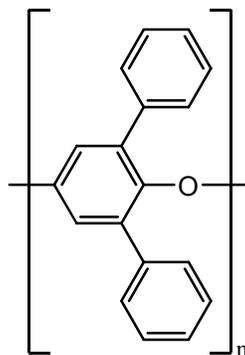
The distinction of enantiomers is analogous to the distinction that would occur if you considered putting your feet into only one of your shoes. If you put your left foot into your left shoe, it feels fine. If you put your right foot into your left shoe, it does not fit quite as well, and even in the dark, you would notice that something isn't right. If we expressed this as a reaction with an equilibrium constant, we could say that the association of your left foot with your left shoe is higher than the association of your right foot with your left shoe. If we had bonded the left shoes to silica gel, your right foot would elute faster from the column, your left foot slower. The compound pictured above has a number of groups that can form intermolecular interactions with enantiomeric solutes. The amide functionality is a site with dipoles and the potential for hydrogen bonding. The electron-deficient dinitrobenzoyl ring can undergo what is known as π -stacking with electron-rich aromatic rings. The isobutyl group of the leucine provides steric hindrance. Other chiral liquid chromatographic phases are designed to have similar groups that provide sites for intermolecular attraction, π -stacking, and steric constraints.

GAS CHROMATOGRAPHIC SEPARATION METHODS

A gas chromatograph typically has a carrier gas (it is common to refer to the mobile phase in gas chromatography as the carrier gas since the mobile phase has no influence at all over the separation – its only purpose is to carry the solutes through the column), heated injection port, column in a heated oven, and detector.

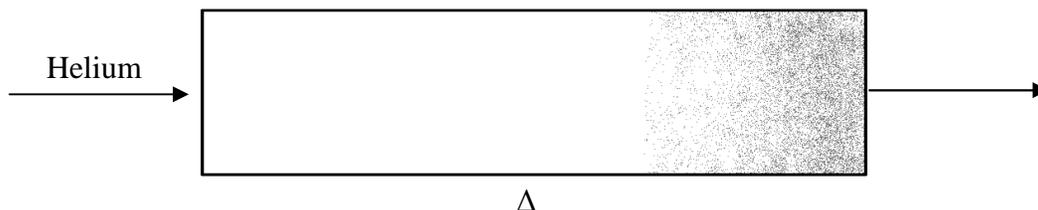
The **carrier gas** must be inert and helium or nitrogen is used for most gas chromatographic applications. Sample injection is most commonly accomplished through the use of a small-volume syringe (1 μL is a typical injection volume). The liquid sample is injected into a hot zone that is sealed with a polymer septum. The syringe pierces the septum, and on injection the liquid sample is flash-volatilized in the heated injection port and flushed into the column by the carrier gas. With fused silica capillary columns, 1 μL of liquid sample will overload the column so the injector is designed with a splitter. Adjusting the flow of the splitter gas allows you to calibrate the split ratio. Ratios of 50:1 to 100:1 (only the one part is injected) are common. Most injection ports of this type have glass liners. Different glass liners are inserted under the septum depending on whether you are doing split or splitless injections.

Another gas chromatographic injection technique that is used in certain applications involves **thermal desorption from a polymer trap**. The technique can be illustrated below for the analysis of organic chemicals in air. Assume that we have a small piece of tubing filled with a polymer. The polymer is a material that organic chemicals will adsorb to. Water in the air will pass through unretained. A polymer that is used quite frequently for this application is Tenax. Tenax is a *p*-polyphenylene oxide polymer that is stable at very high temperatures. In the adsorption step, we use a pump to draw some large volume of air (this might be as high as 15 liters of air) through the Tenax trap, which is held at room temperature. The organic chemicals from the air will adsorb onto the polymer.



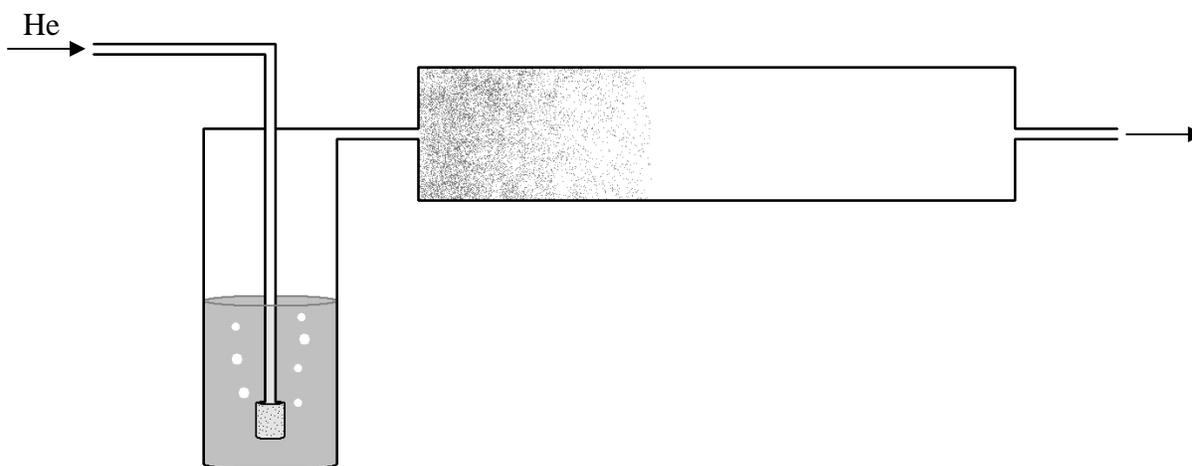
p-polyphenylene oxide

The organic chemicals can be desorbed from the Tenax trap by heating the gas under a flow of helium. The illustration below shows how the Tenax trap is desorbed in a backflush mode (the end that had the higher concentrations of organic chemicals is put closer to the gas chromatograph). Switching valves comparable to liquid chromatographic injection valves make it easy to redirect the flow of gases through these Tenax traps between the adsorption and backflushing orientation.



Desorption might typically be done at a temperature of 225°C over a period of five minutes. One thing to realize is that we would never be able to tolerate a five-minute injection of a sample, since this would mean that all of the peaks might be as long as five minutes. It is essential to maintain a “plug” injection, which is achieved by thermal focussing. **Thermal focussing** is accomplished by cooling a region in the injector (or in older gas chromatographs, the entire oven) to a temperature of -50°C. This cooling is accomplished using either liquid carbon dioxide or liquid nitrogen. At -50°C, the organic compounds that desorb from the Tenax trap freeze in a small band at the head of the column. Rapid heating of this frozen band injects the sample at a comparable rate to a normal syringe injection.

Sorbent traps are frequently used for the analysis of trace levels of volatile organic chemicals in water as well. In this case, the method is known as a purge and trap technique. A sample of water is taken (usually 5 mL – too large to ever inject into a gas chromatograph) and purged with helium gas. After exiting the water, the helium gas flows through a Tenax trap. The helium gas bubbling through the water displaces the dissolved volatile organic chemicals, which adsorb onto the Tenax trap. The Tenax trap is desorbed as described above for the analysis of volatile organic chemicals in air.



Information on a variety of commercially available gas chromatographic stationary phases is shown below. The distinction between different stationary phases is based on a comparison of their polarity. Five different compounds are typically used to represent different types of functional groups. Individual indices for these five compounds are measured, and a composite value (P) is determined as well. These polarity indices are referred to as Rohrschneider constants. The higher the number the more polar the phase. In reality, a sampling of four or five stationary phases would be good enough to span the range of polarities that is needed for gas chromatographic separations.

Rohrschneider Constants for Gas Chromatographic Liquid Phases

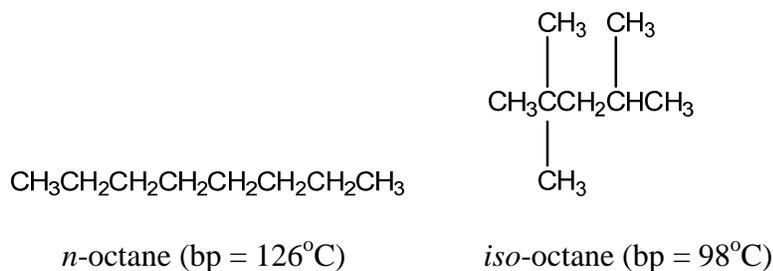
Liquid phase	Max T	X'	Y'	Z'	U'	S'	P
	°C						
Squalane	100	0	0	0	0	0	0
Apiezon L	250	32	22	15	32	42	29
SE-30	300	15	53	44	64	41	43
OV-1, methyl gum	350	16	55	44	65	42	44
OV-3, 10% phenyl	350	44	86	81	124	88	85
OV-7, 20% phenyl	350	69	113	111	171	128	118
Dioctyl sebacate	125	72	168	108	180	123	130
Dilauryl phthalate	-	79	158	120	192	158	141
Dinonyl phthalate	150	83	183	147	231	159	161
OV-17, 50% phenyl	375	119	158	162	243	202	177
Versamid 930	150	109	313	144	211	209	197
Trimer acid	150	94	271	163	182	328	218
OV-25, 75% phenyl	350	178	204	208	305	280	235
Polyphenylether	225	182	233	228	313	293	250
Triton X-305	200	262	467	314	488	430	392
Carbowax 20M	225	322	536	368	572	510	462
Carbowax 4000	200	317	545	378	578	521	468
Reoplex 400	200	364	619	449	647	671	550
Carbowax 1540	175	371	639	453	666	641	554
Diglycerol	100	371	826	560	676	854	657
EGSS-X	200	484	710	585	831	778	678
Ethylene glycol phthalate	200	453	697	602	816	872	688
Diethylene glycol succinate	200	496	746	590	837	835	701
Tetrahydroxyethylenediamine	150	463	942	626	-	893	731
Hexakis(2-cyanoethoxycyclohexane)	150	567	825	713	978	901	797
N,N-bis(2-cyanoethyl)formamide	125	690	991	853	1110	1000	929

X' = benzene; Y' = butanol; Z' = 2-pentanone; U' = nitropropane; S' = pyridine
 $P = (X' + Y' + Z' + U' + S')/5$

If we consider **what governs retention order in gas chromatography**, there are two important parameters. One is the volatility of the compound, with the observation that more volatile compounds (those with a higher vapor pressure or lower boiling point) elute first. The other is the attractive forces between the compound and the stationary phase. If we consider the homologous series of alcohols listed below, it's interesting to note that the boiling point goes up by approximately 20°C for each additional methylene group (CH₂) in the chain. The increase in boiling point with each additional methylene group is a little higher for the series of alkanes. The alcohols have higher boiling points than the corresponding alkanes because they can hydrogen bond with each other.

Hydrocarbon	Boiling Point (°C)	Alcohol	Boiling Point (°C)
Pentane	36	1-Pentanol	137
Hexane	69	1-Hexanol	157
Heptane	98	1-Heptanol	176
Octane	126	1-Octanol	196
Nonane	151	1-Nonanol	215
Decane	174	1-Decanol	231

If we consider a homologous series, it turns out that the boiling points are actually determined by the molar volumes of the molecules. Just as we observed with the size of molecules in steric exclusion chromatography, the molar volume of a molecule is the volume swept out by the molecule as it tumbles. Molecules with larger molar volumes have higher boiling points, provided the molecules being compared have identical intermolecular forces (you cannot compare hydrocarbons to alcohols). An interesting comparison is observed by looking at the boiling point of *n*-octane and *iso*-octane (2,2,4-trimethylpentane).



The branched *iso*-octane would have a smaller molar volume than the linear *n*-octane, and this is clearly reflected in the boiling points of the two compounds.

When predicting retention order in gas chromatography, the overriding factor is a comparison of the boiling points. The compound with the lowest boiling point will elute first. Only when two compounds have very close boiling points (within 5°C or less) does it become important to consider the polarity of the compounds relative to the polarity of the stationary phase. Remember that like dissolves like, so a polar stationary phase will show more retention of a polar compound. The Rohrschneider values are used to determine the polarity of the stationary phase.

Detection Methods

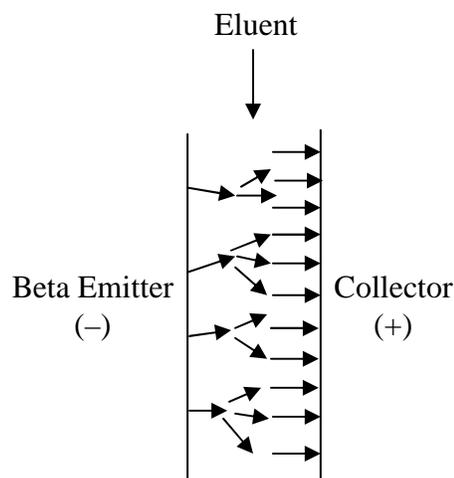
As mentioned previously, highly sensitive detection methods were developed for gas chromatography in the 1950s and 1960s that facilitated its use as an analytical method.

One of the most useful detection methods is known as the **flame ionization detector (FID)**. The flame ionization detector is highly sensitive and involves burning the sample in an air-hydrogen flame. Molecules with a CH bond will form CH^+ ions in the flame, and these are measured using a negatively charged collector above the flame. When these positive ions strike the negatively charged collector, a current proportional to the amount of ions is measured. This detector is essentially universal, as it is able to measure all organic compounds. It is not sensitive toward compounds like water and carbon dioxide, which is advantageous.

Another important detector in the development of gas chromatography is the **thermal conductivity detector**. This is a universal detector, but not nearly as sensitive as the FID. A resistance circuit called a Wheatstone bridge is used. The bridge has two halves, and the resistance of these halves is compared. Instruments with a thermal conductivity detector need two matched columns. One column has only carrier gas flowing through it. The other has carrier gas and sample. Changes in the thermal conductivity of the gas change the resistance reading over the Wheatstone bridge. Some representative values for thermal conductivities of gases are listed below. The value for butane is representative of most organic compounds. Since we need to measure a difference in thermal conductivity, we need a carrier gas with as different a thermal conductivity as possible from most organic compounds. This would suggest the use of hydrogen gas as a carrier gas, however hydrogen is too much of an explosion risk for this purpose. Helium is therefore the carrier gas of choice. Thermal conductivity detectors tend to be used on less expensive pieces of equipment like the gas chromatographs used for the analysis of the purity of compounds prepared in organic chemistry instructional labs.

Thermal conductivity values:	Hydrogen	471
	Helium	376
	Nitrogen	66
	<i>n</i> -Butane	43

One of the most important gas chromatographic detectors ever developed was the **electron capture detector**. This device, which is illustrated below, was invented by James Lovelock, a British chemist. The device has a radioactive foil (usually containing tritium or radioactive nickel) that emits beta particles. Beta particles are high-energy electrons emitted by a nuclear decay process (a neutron decays into a beta particle and a proton). The opposite side of the device is positively charged so the beta particles stream across the tube. As the high-energy beta particles strike carrier gas molecules (usually either nitrogen or an argon/methane mixture), they create a cascade of lower energy electrons, which generate a current that can be measured. If we had a compound coming out of the gas chromatograph that could capture some of these low-energy electrons, the current would drop. The drop in current can be related to the concentration of electron capturing compound in the sample. What is especially impressive about this detector is the level of sensitivity that can be achieved for certain classes of compounds.

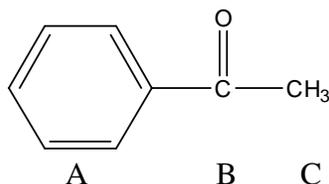


What types of compounds ought to have the ability to capture electrons? Remembering back to your knowledge of periodic properties, you should predict that halogen-containing compounds (compounds with a chlorine, fluorine, or bromine atom) ought to be very effective at capturing electrons. What are especially significant are the classes of compounds that contain halogens. These include the following (with their respective application or concern):

- Chlorofluorocarbons (or freons) – ozone layer destruction
- Chloroform – potential carcinogen formed in drinking water from water chlorination
- Dioxin – by-product of combustion and certain industrial processes
- Chlorinated pesticides such as DDT
- Polychlorinated biphenyls – used in electronic devices (transformers)

These are only some examples, but they form an extensive array of compounds of environmental significance. The invention of the electron capture detector facilitated the discovery that freons were making their way to the stratosphere and leading to the destruction of the ozone layer. Without this detector, this discovery would have been delayed by many years.

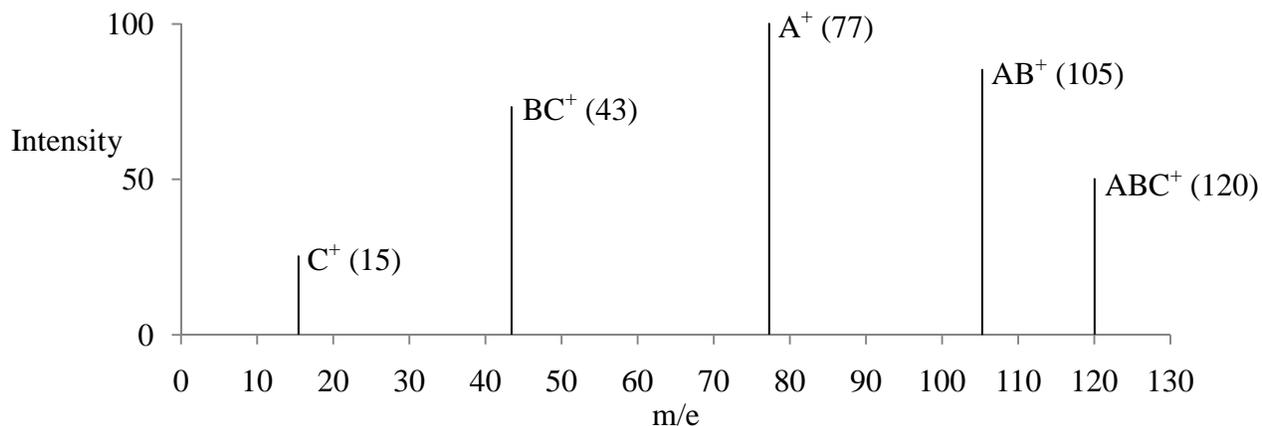
Mass spectrometric detection is especially important because it provides information that can be used for compound identification. Most gas chromatograph-mass spectrometers (GC-MS) use fused silica capillary columns, and the column effluent can go straight into the mass spectrometer. What happens in the mass spectrometer is that the column effluent is bombarded with a high-energy beam of electrons. As these electrons strike the sample, they generate ions. These can be anions or cations, but most mass spectrometers are designed to draw off only the cations for analysis. Usually almost all the cations have a +1 charge. If we consider the molecule shown below, which is known as acetophenone, we can illustrate what will take place (three functional groups within the molecule are labeled A, B, and C).



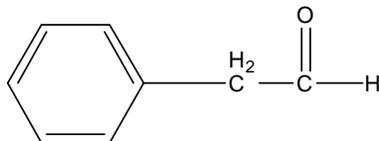
If an electron struck this molecule and knocked out one other electron, we would have the entire molecule with a +1 charge. This ion is referred to as the molecular ion, and we would show this as ABC^+ . It's usually very desirable to have a molecular ion in the spectrum. The other valuable observation in mass spectrometry when you use an electron beam for ionization is that you get fragment ions as well. Fragments we could get from this are listed below, along with their masses. Actually, what is really measured is the mass-to-charge ratio, denoted as m/e . If all of the ions have a charge of +1, the mass equals the mass-to-charge ratio.

<u>Ion</u>	<u>m/e</u>
ABC^+	120
AB^+	105
AC^+	92
A^+	77
BC^+	43
B^+	28
C^+	15

A good question to ask is whether we would ever get AC^+ as a fragment? This would require an intramolecular reaction to take place. This does happen with some molecules, but not the one we are using as an example. Similarly, it might be very unlikely to get a B^+ ion, which would require the loss of two groups. If you were to examine a book on reaction mechanisms that occur in a mass spectrometer, you would notice that it would look very similar to an organic chemistry textbook. The two things we observe is that different fragments have different weights, but they also have different intensities. For example, if a molecule has a good leaving group, it will tend to leave in the mass spectrometer. Depending on which fragment is more stable as a positive ion, the relative intensity of the two ions will vary. The most intense ion is given a value of 100 and the intensity of each other ion is reported relative to it. A possible mass spectrum for acetophenone is provided below. It is worth noting that there will be many more ions in the spectrum than these. For one thing, isotope effects show up. It turns out that 1% of all carbon is carbon-13 so one out of every hundred molecules weighs one more (meaning that we will see a small peak at $m/e = 121$). Note that the mass spectrometer does not measure an average molecular weight based on isotopic abundance, but the exact weight of each ion. For another thing, the molecule might lose a hydrogen atom and show a fragment with a mass of 119.



Notice how we could use these masses to determine a possible molecular formula for the compound, and the masses of fragments to determine possible groups that are found in the molecule. The compound below has the exact same molecular weight (120), but you might appreciate that it would probably have a different mass spectrum.



Mass spectra are relatively difficult to interpret and to assign an unequivocal structure to. What is usually done instead is that the mass spectrometers with a GC-MS come with a library of spectra of known compounds. The computer will compare your measured mass spectrum to those in the library and report the ten best matches. The top match does not confirm the assignment. To do that, you would need an authentic sample of that compound and would have to show that it has the same retention time and mass spectrum on your instrument. With those two matches, you can be assured that you have identified the compound. GC-MS is commonly used for drug testing at sports events like the Olympics.

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Appendix I: Derivation of the Fundamental Resolution Equation

$$R_S = \frac{2(t_2 - t_1)}{W_1 + W_2} \quad (1)$$

$$W_1 \cong W_2$$

$$W = 4\sigma$$

$$R_S = \frac{2(t_2 - t_1)}{8\sigma_2} = \frac{t_2 - t_1}{4\sigma_2} \quad (2)$$

$$N = \left(\frac{t_2}{\sigma_2}\right)^2 \quad \sigma_2 = \frac{t_2}{\sqrt{N}}$$

$$R_S = \frac{t_2 - t_1}{4\left(\frac{t_2}{\sqrt{N}}\right)} \quad (3)$$

$$R_S = \left(\frac{\sqrt{N}}{4}\right)\left(\frac{t_2 - t_1}{t_2}\right) = \left(\frac{\sqrt{N}}{4}\right)\left(1 - \frac{t_1}{t_2}\right) \quad (4)$$

Write an expression for the fraction of material in the mobile phase (ϕ_M):

$$\phi_M = \frac{C_M V_M}{C_M V_M + C_S V_S} \quad (5)$$

$$\phi_M = \frac{\frac{C_M V_M}{C_M V_M}}{\frac{C_M V_M}{C_M V_M} + \frac{C_S V_S}{C_M V_M}} = \frac{1}{1 + k'} \quad (6)$$

Express the average migration velocity of component 2:

$$v_{S_2} = \phi_M v \quad (7)$$

(where v is the mobile phase velocity)

$$v_{S_2} = \frac{L}{t_2} \quad (8) \quad v = \frac{L}{t_0} \quad (9)$$

$$\frac{L}{t_2} = \frac{L}{t_0} \phi_M \quad (10)$$

$$t_2 = \frac{t_0}{\phi_{M_2}} \quad t_1 = \frac{t_0}{\phi_{M_1}} \quad (11)$$

$$t_2 = \frac{t_0}{\left(\frac{1}{1+k_2'}\right)} \quad t_1 = \frac{t_0}{\left(\frac{1}{1+k_1'}\right)} \quad (12)$$

$$t_2 = t_0(1+k_2') \quad t_1 = t_0(1+k_1') \quad (13)$$

$$\frac{t_1}{t_2} = \frac{t_0(1+k_1')}{t_0(1+k_2')} = \frac{1+k_1'}{1+k_2'} \quad (14)$$

Substitute (14) into (4):

$$R_S = \left(\frac{\sqrt{N}}{4}\right) \left(1 - \frac{1+k_1'}{1+k_2'}\right) \quad (15)$$

Consider the $\left(1 - \frac{1+k_1'}{1+k_2'}\right)$ term:

$$\left(1 - \frac{1+k_1'}{1+k_2'}\right) = \left(\frac{1+k_2'}{1+k_2'} - \frac{1+k_1'}{1+k_2'}\right) \quad (15a)$$

$$= \frac{k_2' - k_1'}{1+k_2'} \quad (15b)$$

$$= \frac{k_1' \left(\frac{k_2'}{k_1'} - 1\right)}{1+k_2'} \quad (15c)$$

$$= \frac{\left(\frac{k_2'}{k_1'}\right) k_1' \left(\frac{k_2'}{k_1'} - 1\right)}{\left(\frac{k_2'}{k_1'}\right) (1+k_2')} = \frac{k_2' \left(\frac{k_2'}{k_1'} - 1\right)}{\left(\frac{k_2'}{k_1'}\right) (1+k_2')} \quad (15d)$$

$$= \left(\frac{k_2'}{1+k_2'}\right) \left(\frac{\frac{k_2'}{k_1'} - 1}{\frac{k_2'}{k_1'}}\right) \quad (15e)$$

$$\alpha = \frac{k_2'}{k_1'}$$

$$= \left(\frac{k_2'}{1+k_2'}\right) \left(\frac{\alpha - 1}{\alpha}\right) \quad (15f)$$

Substitute (15f) into (15):

$$R_S = \left(\frac{\sqrt{N}}{4}\right) \left(\frac{\alpha - 1}{\alpha}\right) \left(\frac{k_2'}{1 + k_2'}\right)$$

Relationship to retention time:

$$v_{S_2} = \frac{L}{t_2} \quad t_2 = \frac{L}{v_{S_2}}$$

$$v_{S_2} = \phi_M v = \left(\frac{1}{1 + k_2'}\right) v \quad (16)$$

$$H = \frac{L}{N} \quad L = HN$$

$$t_2 = \frac{HN(1 + k_2')}{v} \quad (17)$$

Rearrange the fundamental resolution equation to solve for N:

$$N = 16R_S^2 \left(\frac{\alpha}{\alpha - 1}\right)^2 \left(\frac{1 + k_2'}{k_2'}\right)^2$$

$$t_2 = \left(\frac{16R_S^2 H}{v}\right) \left(\frac{\alpha}{\alpha - 1}\right)^2 \left(\frac{(1 + k_2')^3}{(k_2')^2}\right) \quad (18)$$